

Global Deep Ocean Observations of Horizontal Eddy–Mean Interactions of Temperature Variance

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ABSTRACT: Ocean eddies are ubiquitous in the ocean. Characterizing and quantifying their impact on the large-scale ocean circulation is key. Here, we compute eddy–mean interactions for Conservative Temperature variance, including temperature variance transfers. This is done using the ANDRO dataset, which records mean temperature and horizontal displacement of Argo floats during their journey at parking depth (~ 1000 m). The analysis does not show any consistency between the sign of the turbulent heat flux and the slope of the mean isotherms, questioning the validity of traditional downgradient flux turbulent closure in the context of the temperature variance budget. The temperature variance interactions suggest the dominance of the nonlocal, redistribution term over the local, transfer term. They both have typical spatial scales ranging from 200 to 1000 km. When averaged over large regions, transfers are from the mean to the turbulence, but the northwest Atlantic remains a unique region which acts as a turbulence graveyard. Within a water-mass framework, transfers are quite consistently shrinking the mean temperature distribution except for a few extreme water masses: the Arctic Intermediate Water, the Antarctic Bottom Water, and the Red Sea–Persian Gulf Intermediate Water. This is also the case for a subset of the Mediterranean Water. However, the Mediterranean Water is the main location of the sharpening of the mean temperature distribution. These results provide observational evidence of the action of the turbulence on the mean temperature structure that could be tested in numerical ocean and climate models for validation and for the development and the implementation of ocean turbulent closures.

KEYWORDS: Ocean; Mesoscale processes; Ocean circulation; Oceanic profilers; In situ oceanic observations

1. Introduction

Since the preindustrial era, climate is changing at an unrecorded pace (IPCC 2021). This is true for all its components, including the ocean that has stored 90% of the heat excess (von Schuckmann et al. 2023). This heat changes the large-scale ocean temperature structure. To further anticipate this change, it becomes more and more timely to better understand the dynamics and the physical process controlling this large-scale ocean temperature structure. In parallel, one of the most energetic features, that is ubiquitous in the ocean (Chelton et al. 2007), is the mesoscale eddy turbulence (Ferrari and Wunsch 2009). Hence, understanding how this energetic turbulence and the large-scale temperature structure interact is the central question of this study.

There is a long history of studying eddy–mean flow interactions in the fields of ocean and atmospheric research. We could cite the negative viscosity concept of Starr (1968), rationalizing the eddy-driven character of the midlatitude westerlies, or the eddy-forced nature of the inertial recirculation of the Gulf Stream, established by Holland (1978) and Rhines and Holland (1979). Focusing on the temperature, it is well accepted that mean temperature gradients, through their effect on density, contribute to feeding eddy turbulence through baroclinic instability (Charney 1947; Eady 1949). However, this turbulence impacts the temperature field through isopycnal eddy diffusion (McDougall and McIntosh 2001; McDougall et al. 2014;

Groeskamp et al. 2020; Sévellec et al. 2022, 2025b). This is typical evidence of the two-way eddy–mean flow interactions for temperature. However, this classical and somehow plausible description remains quite qualitative. A more analytical and robust approach to quantitatively characterize the eddy–mean interactions for temperature is thus required.

A robust framework for identifying global-average eddy–mean flow interactions has been developed by Lorenz (1955). This has been extensively used in the oceanographic community to study the interactions between the mean and the eddy kinetic energy (e.g., Ferrari and Wunsch 2009). However, when applied locally, this global framework suffers from an apparent discrepancy between the local gain/loss of the mean energy reservoir and the local loss/gain of the eddy energy reservoir. This has been rationalized through the definition of a ghost reservoir (residual kinetic energy) acting as a mediator between the mean and eddy kinetic energy (Murakami 2011; Murakami et al. 2011; Chen et al. 2014, 2016; Kang and Curchitser 2015; Yan et al. 2019; Matsuta and Masumoto 2021; Jamet et al. 2022; Sévellec et al. 2025a). However, these studies do not focus on tracers and are thus not directly generalizable to temperature. Hence, in parallel to these studies, there exists a wide range of studies on tracer variance budgets (Sévellec et al. 2006; Arzel et al. 2006; Buckley et al. 2012; Hochet et al. 2020; Sévellec et al. 2021; Hochet et al. 2023, 2024b, 2026). This framework allows one to quantitatively estimate sources and sinks of tracer variance. However, these studies do not relate the mean and the eddy temperature. Hochet et al. (2024a) attempted to rationalize the link between mean reservoir gain and loss and eddy reservoir loss and gain, respectively. Whereas their suggestion

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is perfectly valid for global interpretation, they face the same local issue than the one discussed above for kinetic energy. They find an inconsistency between the gain and loss of tracer variance by the mean and eddy reservoirs. Hence, a consistent framework, analogous to the one for kinetic energy and valid for local interactions but tailored for temperature, is needed.

Indeed, there are specific scientific questions and challenges for the temperature budget. This could be illustrated by starting from the evolution equation for Conservative Temperature. This reads the following:

$$D_t \Theta = F_\Theta + D_\Theta, \quad (1)$$

where Θ is the Conservative Temperature (McDougall and Barker 2011), D_t is the material derivative, and F_Θ and D_Θ are the surface atmospheric forcing and small-scale dissipative terms. The material derivative reads $D_t = \partial_t + \mathbf{u}^\dagger \cdot \nabla$, where t is time, $\mathbf{u}^\dagger = (u, v, w)$ is the three-dimensional velocity vector (with u , v , and w being the zonal, meridional, and vertical velocities, and $\nabla^\dagger \cdot \mathbf{u} = 0$ ensuring the nondivergence of the flow), $\nabla^\dagger = (\partial_x, \partial_y, \partial_z)$ is the three-dimensional derivative operator (with x , y , and z being the longitude, latitude, and depth), $\cdot$ is the three-dimensional scalar product, and † is the transpose operator. Based on this equation and an ad hoc derivation using a water-mass framework (Walín 1982), Zika et al. (2015) suggested that the water-mass distribution is controlled by an equilibrium between the forcing term and the dissipation. Indeed, intuitively, if the dissipation term is a diffusion, by mixing waters it removes the differences and sharpens the distribution. In the case of diffusion represented by downgradient fluxes, it is indeed trivial. Hence, only the forcing term remains to maintain temperature differences and broaden the distribution. This is equivalent to an inflection point in the temperature–salinity diagram due to the “stirring” of water types (i.e., temperature–salinity properties at their origin/formation). However, if one is interested in some kind of spatio-temporal average rather than a local/instantaneous value, (1) would be modified to include a turbulent term. Hence, all the previous neat arguments would fail if this term were not equivalent to a diffusion characterized by downgradient fluxes. For instance, if the turbulent term acts as a negative diffusivity, similarly to the so-called negative viscosity described by Starr (1968), it would broaden the temperature distribution. To clarify this, in the present study, we will derive the exact equation controlling the broadening/sharpening of the spatiotemporal average ocean temperature distribution. We will then describe the impact of mesoscale turbulence on the distribution of temperature in the ocean.

To this purpose, we will use the ANDRO dataset (Ollitrault and Rannou 2013), which provides concomitant horizontal velocity and temperature observations measured during the deep displacements of Argo floats. To diagnose eddy–mean interactions with this dataset, we will develop a framework describing the interactions between the mean temperature variance and the eddy temperature variance. Equivalently to the description of eddy–mean flow interactions for kinetic energy, we will show the existence of local and nonlocal interactions. The former

corresponds to variance transfers, whereas the latter corresponds to variance redistribution. Application of the framework to the dataset shows that the eddy turbulence tends, on average, to smooth mean temperature differences [as hypothesized by Zika et al. (2015)] but not locally.

The manuscript is organized as follows. In section 2, the ANDRO dataset is described. In section 3, the theoretical framework is derived, and restriction to a horizontal framework is discussed. The results are presented in section 4. We conclude with discussions of our results in section 5.

2. The ANDRO dataset

In this study, we have used temperature records and velocity estimations from Argo float deep displacements. By using temperature recorded during deep displacements, rather than during vertical profiles, we have consistent observations of temperature and velocities. These observations are provided by the ANDRO dataset (Ollitrault et al. 2026). In particular, we used the No. 116520 release of 2025. It has all the Argo float deep drifts from 2000 to 2009 but is only partially complete for 2010–25. This dataset corresponds to 1 678 510 observations, but when selecting the studied pressure range (950–1150 dbar), we find 1 248 238 observations (Fig. 1a). In the rest of the study, we will consider this depth to be ~ 1000 m. When limiting the range of temperature to between -2° and 13°C (to avoid erroneous data), we obtain 1 221 746 observations. This leads to a mean observation density of 144.0 observations per $2^\circ \times 2^\circ$ with a standard deviation of 87.9 observations per $2^\circ \times 2^\circ$ and a maximum observation density reaching 915 observations per $2^\circ \times 2^\circ$ (Fig. 1b).

Using these velocity and temperature records, we computed the mean zonal velocity, meridional velocity, and Conservative Temperature fields on a $1^\circ \times 1^\circ$ grid as

$$\bar{u} = \frac{1}{n} \sum_{i=1}^n u_i, \quad (2a)$$

$$\bar{v} = \frac{1}{n} \sum_{i=1}^n v_i, \quad (2b)$$

$$\bar{\Theta} = \frac{1}{n} \sum_{i=1}^n \Theta_i, \quad (2c)$$

where u_i and v_i are individual deep zonal and meridional velocity records, respectively, Θ_i is an individual deep Conservative Temperature record, i is the index of the record, and n is the total number of records within a $2^\circ \times 2^\circ$ cell centered on a $1^\circ \times 1^\circ$ grid point.

We can also compute the unbiased variance of these fields:

$$\overline{u'^2} = \frac{1}{n-1} \sum_{i=1}^n (u_i - \bar{u})^2, \quad (3a)$$

$$\overline{v'^2} = \frac{1}{n-1} \sum_{i=1}^n (v_i - \bar{v})^2, \quad (3b)$$

$$\overline{\Theta'^2} = \frac{1}{n-1} \sum_{i=1}^n (\Theta_i - \bar{\Theta})^2. \quad (3c)$$

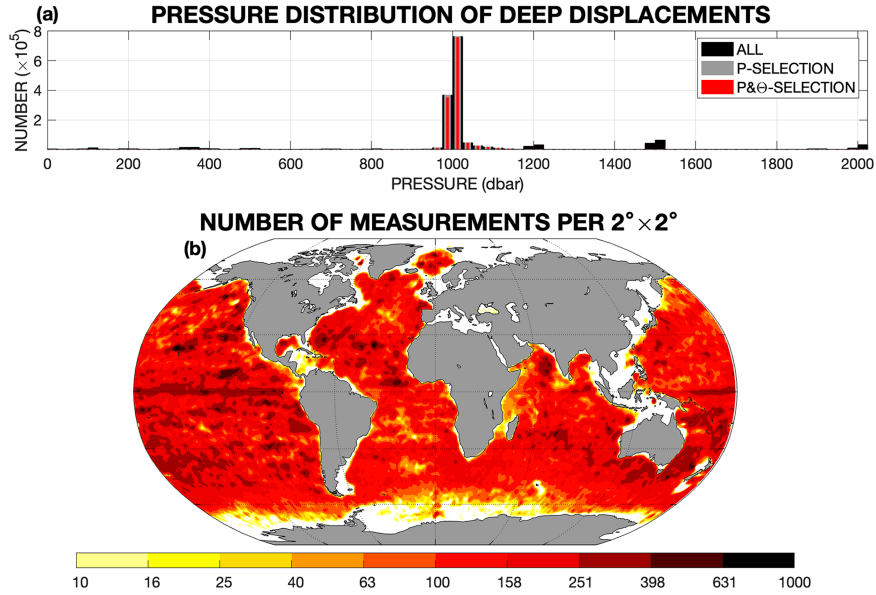


FIG. 1. Distribution of velocity observations from the ANDRO dataset. (a) Distributions of the parking depth pressure of the Argo float deep displacements from the ANDRO dataset (#116520). Two sequential selections of observations: “*P*-selection” corresponding to a range of pressure (from 950 to 1150 dbar) and “*P*&*Θ*-selection” corresponding to both the range of pressure and a range of Conservative Temperature (from -2° to 13°C). (b) Number of *P*&*Θ*-selected deep velocity observations per $2^{\circ} \times 2^{\circ}$. Note the logarithmic color scale.

An estimation of the deep horizontal mean and eddy kinetic energy can then be obtained as $\text{MKE} = (\bar{u}^2 + \bar{v}^2)/2$ and $\text{EKE} = (\overline{u'^2} + \overline{v'^2})/2$.

Following the same principle, we define the unbiased covariances of the zonal and meridional velocities with the Conservative Temperature. This reads

$$\overline{u'\Theta'} = \frac{1}{n-1} \sum_{i=1}^n (u_i - \bar{u})(\Theta_i - \bar{\Theta}), \quad (4a)$$

$$\overline{v'\Theta'} = \frac{1}{n-1} \sum_{i=1}^n (v_i - \bar{v})(\Theta_i - \bar{\Theta}). \quad (4b)$$

At 1000 m, we find mean Conservative Temperature going from -1.8°C in the Nordic seas to 11.8°C along the Portugal coast and in the Gulf of Aden (Fig. 2a). In the Southern Ocean, we obtain water down to 0.5°C , whereas it is 2.5° and 3.3°C in the Pacific and the Atlantic, respectively. This is consistent with state-of-the-art knowledge of descriptive oceanography (Talley et al. 2011). Following Emery (2018), we find a range of water masses at this depth: the Antarctic Bottom Water (AABW), the Circumpolar Deep Water (CDW), the Antarctic Intermediate Water (AAIW), the Mediterranean Water (MW), the Red Sea–Persian Gulf Intermediate Water (RSPGIW), the North Atlantic Deep Water (NADW), and the Arctic Intermediate Water (AIW). The temperature variance shows values of up to 3 K^2 , localized in the Agulhas retroflexion and return current, in the Gulf Stream and its continuation as the North Atlantic Current, in the Antarctic Circumpolar Current, and in the North Brazilian Current retroflexion (Fig. 2b). In terms of momentum, the mean and eddy kinetic energy (MKE and EKE)

have values of up to 10^{-2} and $2 \times 10^{-2} \text{ m}^2 \text{ s}^{-2}$, respectively. They are strong in intense western boundary currents (e.g., the Gulf Stream, Kuroshio, Zapiola Gyre, and Agulhas Current and its retroflexion), as well as in the Antarctic Circumpolar Current (ACC) (Figs. 2c,d). EKE is also strong in the equatorial region. This was already reported with an older version of the same dataset (No. 109566) by Sévellec et al. (2025a).

Using error estimates of the individual velocities provided by the ANDRO dataset (Ollitrault et al. 2026), full error estimation has been provided in Sévellec et al. (2024, 2025a). This includes observation error (primarily controlled by the Argo float positioning error at 1000 dbar), sample size error, and error introduced by the grid-scale choice of the analysis. We refer the readers to these two studies for details. Overall, these error estimations show the robustness of analyses based on the mean and the variance. This directly derives from the high number of individual observations within $2^{\circ} \times 2^{\circ}$ cells (Fig. 1) and the good convergence of simple statistics, such as the mean and the variance. As in Sévellec et al. (2024, 2025a), in the rest of the study, we will only use the mean and the variance. It is also worth noting that despite being Lagrangian observations, the ANDRO dataset has been shown to lead to results consistent with Eulerian analyses, as for isopycnal diffusivity coefficient estimates (Sévellec et al. 2022 vs Roach et al. 2018, and Groeskamp et al. 2020), for instance.

3. Theoretical framework

a. General derivations of temperature variance budget

Restarting from (1) and applying the change of variable $T = \Theta - \langle \Theta \rangle$ (where $\langle \cdot \rangle$ is a spatiotemporal average defined over

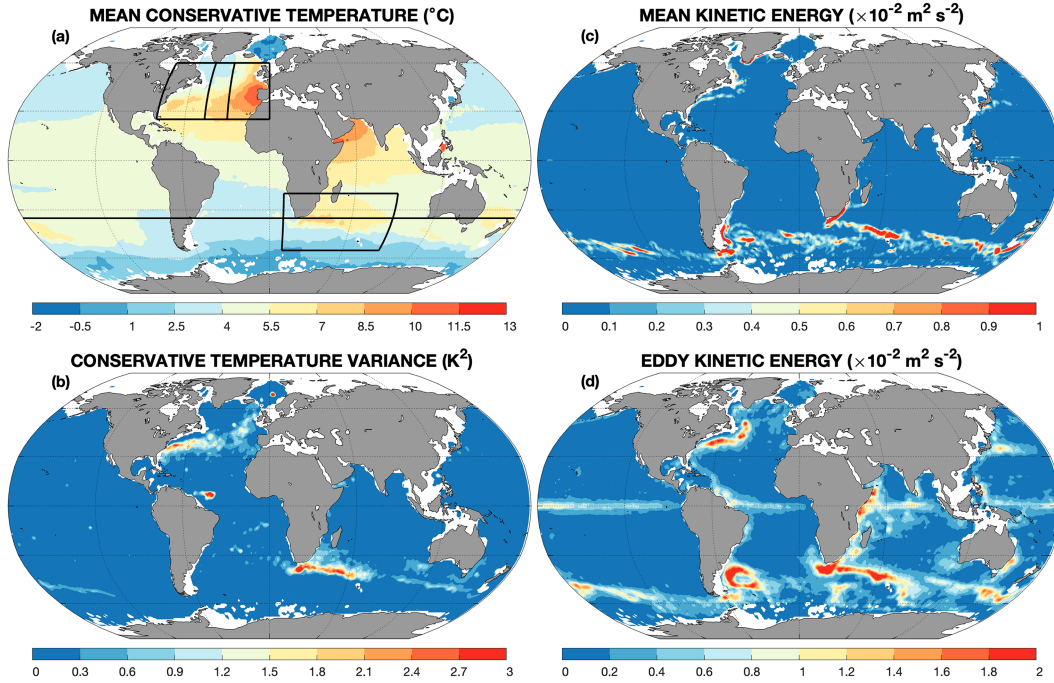


FIG. 2. Conservative Temperature and kinetic energy from Argo float deep displacement observations at 1000-m depth. (a) Mean Conservative Temperature ($\bar{\Theta}$), (b) Conservative Temperature variance ($\bar{\Theta}'^2$), (c) MKE [$\text{MKE} = (\bar{u}^2 + \bar{v}^2)/2$], and (d) EKE [$\text{EKE} = (\bar{u}'^2 + \bar{v}'^2)/2$]. The observations have been mapped following (2) and (3). The black line and boxes denote the regions used for spatial averages: west, central, east, and all North Atlantic, Agulhas Current sector, and Southern Ocean sector.

the whole globe and over the full duration of the studied time series), we obtain the time evolution equation for the centered temperature:

$$D_t T = F + D, \quad (5)$$

where F and D are derived from F_Θ and D_Θ , respectively, but have been adapted for the change of variable. Note that $D \equiv D_\Theta$, if D_Θ has the form of a Laplacian. Also, note that, if the average is only a horizontal and temporal average ($\langle \cdot \rangle_{\text{hor}}$), defining a mean stratified reference state, as is often done in the context of available potential energy definition (e.g., Lorenz 1955), we have $\partial_z \langle \Theta \rangle_{\text{hor}} \neq 0$, and the forcing F should incorporate a term of the form $-\bar{w} \partial_z \langle \Theta \rangle_{\text{hor}}$ deriving from the advective term (and potentially a term deriving from the diffusive term, although it is often negligible, since the Péclet number is high: $\text{Pe} \gg 1$). This property will be used in section 4d.

From (5) and splitting the temperature and velocity into a statistical mean and an anomaly so that $T = \bar{T} + T'$ and $\mathbf{u} = \bar{\mathbf{u}} + \mathbf{u}'$, where $\bar{T}' = 0$ and $\bar{\mathbf{u}}' = (0, 0, 0)$, we obtain the evolution equation for the mean and anomalous centered temperature:

$$\partial_t \bar{T} + \nabla^i \cdot (\bar{\mathbf{u}} \bar{T}) = \underbrace{-\nabla^i \cdot \bar{\mathbf{u}}' T'}_{\mathcal{C}} + \bar{F} + \bar{D}, \quad (6a)$$

$$\partial_t T' + \nabla^i \cdot (\mathbf{u} T') = -\nabla^i \cdot (\mathbf{u}' \bar{T}) + \underbrace{\nabla^i \cdot \mathbf{u}' T'}_{-\mathcal{C}} + F' + D', \quad (6b)$$

where $\bar{\mathbf{u}}' T' = (\bar{u}' T', \bar{v}' T', \bar{w}' T')$ is the turbulent temperature flux. (Note that $T' = \Theta'$.) This shows the importance of the

divergence of the turbulent temperature flux ($\bar{\mathbf{u}}' T'$) in forcing the mean temperature. This term could also be interpreted as the closure term for the large-scale evolution: $\mathcal{C} = -\nabla^i \cdot \bar{\mathbf{u}}' T'$.

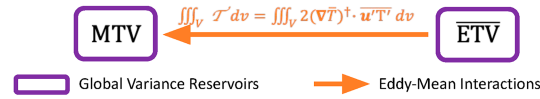
To study the variance, we define three temperature variance reservoirs: the mean, the residual, and the eddy temperature variance reservoirs, so that $\text{MTV} = \bar{T}^2$, $\text{RTV} = \overline{2\bar{T}T'} = 0$, and $\text{ETV} = \overline{T'^2}$ (Fig. 3). This decomposition directly derives from $T^2 = \bar{T}^2 + 2\bar{T}T' + T'^2$. This corresponds to the zeroth-, first-, and second-order anomalies of the temperature square. It is worth noting that the residual reservoir is identically zero on average and could then be considered as a “ghost” reservoir. However, as shown latter, and in analogy with the work of Chen et al. (2014, 2016) in the context of kinetic and potential energy, it is key as residual temperature variance (RTV) acts as a mediator between eddy temperature variance (ETV) and mean temperature variance (MTV). From multiplying (6) with either $\bar{T}$ or T' , we obtain the evolution of these three temperature variance reservoirs. This leads to

$$\partial_t \bar{T}^2 + \nabla^i \cdot \overline{\mathbf{u}' T'^2} = \underbrace{-2\bar{T} \nabla^i \cdot \bar{\mathbf{u}}' T'}_{\mathcal{R}=\mathcal{A}+\mathcal{I}} + 2\bar{T}\bar{F} + 2\bar{T}\bar{D}, \quad (7a)$$

$$\begin{aligned} \partial_t \overline{T'^2} + \nabla^i \cdot \overline{\mathbf{u}' 2\bar{T}T'} &= \underbrace{2\bar{T} \nabla^i \cdot \bar{\mathbf{u}}' T'}_{-\mathcal{R}} + \underbrace{2(\nabla^i \bar{T}) \cdot \bar{\mathbf{u}}' T'}_{\mathcal{T}} \\ &\quad + \underbrace{2\bar{T}(F' + D')}_{=0} + \underbrace{2T'(\bar{F} + \bar{D})}_{=0}, \end{aligned} \quad (7b)$$

TEMPERATURE VARIANCE RESERVOIR INTERACTIONS

GLOBAL VIEW:



LOCAL VIEW:

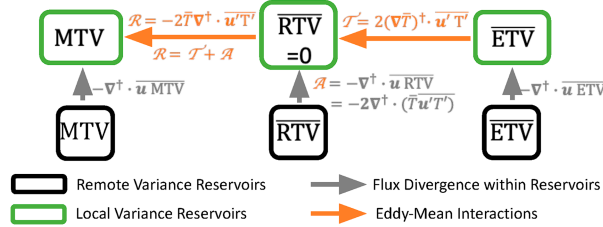


FIG. 3. Schematic of global and local interactions between temperature variance reservoirs. Globally, variance transfers are from ETV ($\overline{ETV} = \overline{T'^2}$) to MTV ($\overline{MTV} = \overline{T'^2}$) through the intrareservoir action of the spatial integral of the eddy-mean interactions, solely controlled by the local component (i.e., $\int \mathcal{R} dv = \int \mathcal{T} dv$). Locally, variance transfers occur both through the intrareservoir action of advection and through the interreservoir action of the eddy-mean interactions. Here, the reservoirs are the MTV ($\overline{MTV} = \overline{T'^2}$), the RTV ($\overline{RTV} = 2\overline{T'T'} = 0$), and the ETV ($\overline{ETV} = \overline{T'^2}$). The eddy-mean interactions correspond to the total component ($\mathcal{R}$) received by MTV, the local component ($\mathcal{T}$) leaving the mean ETV, and the nonlocal component ($\mathcal{A}$) leaving the mean RTV and ensuring that it remains zero at all times despite the existence of RTV eddy advection. By construction, the total component is the sum of the local and nonlocal components ($\mathcal{R} = \mathcal{A} + \mathcal{T}$).

$$\partial_t \overline{T'^2} + \nabla^\dagger \cdot \overline{\mathbf{u}' T'^2} = \underbrace{-2(\nabla \overline{T'})^\dagger \cdot \overline{\mathbf{u}' T'}}_{-\mathcal{T}} + 2\overline{T' F'} + 2\overline{T' D'}. \quad (7c)$$

Here, we find that the eddy-mean interactions, $\mathcal{R} = -2\overline{T'\nabla^\dagger \cdot \mathbf{u}' T'}$, are the sum of the variance redistribution, $\mathcal{A} = -2\nabla^\dagger \cdot (\overline{\mathbf{T}'\mathbf{u}' T'})$, and the variance transfers, $\mathcal{T} = 2(\nabla \overline{T'})^\dagger \cdot \overline{\mathbf{u}' T'}$. Following analogous work done on eddy-mean flow interactions for the kinetic energy reservoirs (Chen et al. 2014, 2016; Sévellec et al. 2025a), we also define $\mathcal{R}$, $\mathcal{A}$, and $\mathcal{T}$ as the total, nonlocal, and local interactions (Fig. 3). In (7), we see the special role of advection for RTV ($\mathcal{A}$). Indeed for MTV and ETV, their respective advection only acts as an intrareservoir action. However, for RTV, because RTV is unambiguously zero on average, this intrareservoir action impacts the interreservoir interactions and accumulates with $\mathcal{T}$ from ETV to impact MTV through $\mathcal{R}$.

Equivalent derivations have been done in the context of energy reservoir exchange of available potential energy ($\propto \rho^2$, where ρ is density) by Kang and Curchitser (2015) and Chen et al. (2016) and of potential energy in a quasigeostrophic model [$\propto (\partial_z \psi)^2$, where ψ is the streamfunction] by Jamet et al. (2024), for instance. These derivations lead to equivalent eddy-mean interaction terms and reservoirs.

From (7), we can retrieve the more classical global view [equivalent to the Lorenz (1955) energy cycle] by integrating over the volume of the ocean. This reads

$$\partial_t \int \int \int_V \overline{T'^2} dv = 2 \int \int \int_V (\nabla \overline{T'})^\dagger \cdot \overline{\mathbf{u}' T'} dv + 2 \int \int \int_V (\overline{T' F'} + \overline{T' D'}) dv, \quad (8a)$$

$$\begin{aligned} \partial_t \int \int \int_V \overline{T'^2} dv = & -2 \int \int \int_V (\nabla \overline{T'})^\dagger \cdot \overline{\mathbf{u}' T'} dv \\ & + 2 \int \int \int_V (\overline{T' F'} + \overline{T' D'}) dv, \end{aligned} \quad (8b)$$

where V is the total ocean volume and dv is the volume element. Here, we only need two reservoirs: the global-mean MTV and ETV. Also, beyond forcing and dissipation, only the eddy-mean interactions remain, since advection terms vanish when globally averaged (as a consequence of mass conservation). Finally, the eddy-mean interactions simplify to $\int \int \int_V \mathcal{R} dv = \int \int \int_V \mathcal{T} dv$, since $\int \int \int_V \mathcal{A} dv = 0$ (again, as a consequence of mass conservation), leading to nonambiguous variance transfers between the mean and the eddy reservoirs. Also, $\int \int \int_V \mathcal{R} dv$ is a direct contributor to the variance of the temperature distribution, showing the impact of the turbulence on the temperature distribution. Indeed, dividing by the global volume, (8a) becomes an equation for the spatial variance of the large-scale temperature ($\sigma_T^2 = \langle \overline{T'^2} \rangle$). This reads

$$\partial_t \sigma_T^2 = \langle \mathcal{T} \rangle + 2\langle \overline{T' F'} \rangle + 2\langle \overline{T' D'} \rangle. \quad (9)$$

This derivation was also provided in the context of freshwater content variation of the Arctic by Hochet et al. (2024a), for instance. In this expression, the forcing term acts as the spatial covariance between temperature forcing and the mean temperature field. Hence, beyond the amplitude, the shape consistency between the temperature forcing and the mean temperature is key in modifying the spatial variance of the large-scale temperature.

At high Péclet number ($Pe \gg 1$ —diffusion is negligible over advection: $\langle \overline{T' D'} \rangle \simeq 0$), the distribution is maintained (i.e., $\partial_t \sigma_T^2 = 0$) by a balance between the forcing and the action of the turbulence:

$$\langle \overline{T' F'} \rangle = -\frac{1}{2} \langle \mathcal{T} \rangle. \quad (10)$$

This is the analytical demonstration of the intuitive description of the maintenance and broadening of the ocean's tracer distribution suggested by Zika et al. (2015), who only proposed an advanced scaling argument.

Even if not of leading order locally (i.e., $Pe \gg 1$), it is possible that the global impact of the diffusive term is key. The small-scale dissipative term is often assumed to take the form of a downgradient flux—Fick's law (Redi 1982): $D = \nabla^\dagger \cdot (\mathbf{K} \cdot \nabla \overline{T})$, where $\mathbf{K}$ is the diffusivity tensor. This diffusivity tensor is positively defined as it measures the spread in time of Lagrangian trajectories (Batchelor 1949; Sévellec et al. 2022), which can only grow statistically. In this case, it can be

shown that the global impact of this term on the mean temperature variance reads

$$\begin{aligned} \langle T\overline{D} \rangle &= \frac{1}{V} \iiint_V \overline{T} \nabla^\dagger \cdot (\mathbf{K} \cdot \nabla \overline{T}) dv \\ &= \underbrace{\frac{1}{2V} \oint_{\Sigma} \boldsymbol{\eta}^\dagger \cdot (\mathbf{K} \cdot \nabla \overline{T}^2) d\sigma}_{=0} - \underbrace{\frac{1}{V} \iiint_V (\nabla \overline{T})^\dagger \cdot \mathbf{K} \cdot (\nabla \overline{T}) dv}_{\leq 0}, \end{aligned}$$

where Σ is the surface bounding the ocean, $d\sigma$ is its surface ocean boundary element, and $\boldsymbol{\eta}$ is the vector normal to this surface. Given that the forcing has been explicitly expressed through F , the variance flux is zero. Since it is a scalar product using a positive definite tensor, the second term is unequivocally lower than or equal to zero at all locations: $-(\nabla \overline{T})^\dagger \cdot \mathbf{K} \cdot (\nabla \overline{T}) \leq 0$ and so also when globally averaged. Hence, here we demonstrate that, under the Fick's law assumption, the small-scale dissipative term leads to the shrinking of the mean temperature distribution ($\partial_t \sigma_T^2 \leq 0$), as also suggested by Zika et al. (2015) in a water-mass transformation framework. Physically, this means that the diffusion mixes water masses until there exists only a single temperature class.

Equivalently to the variance of the mean temperature, we can define the mean variance of the anomaly: $\langle \sigma_T'^2 \rangle = \langle T'^2 \rangle$. Using (8b), its evolution is described by

$$\partial_t \langle \sigma_T'^2 \rangle = -\langle T \rangle + 2\langle T'F' \rangle + 2\langle T'D' \rangle. \quad (11)$$

This equation has already been derived in the context of the large-scale ocean variability by Sévellec et al. (2006), for instance. The same properties can be derived for this mean variance as for the variance of the mean. 1) The forcing acts through the global mean of the correlation between forcing anomaly and the temperature anomaly. 2) Small-scale dissipation can only be a sink of variance if one assumes a downgradient flux closure: $\langle T'D' \rangle = -\langle (\nabla T')^\dagger \cdot \mathbf{K} \cdot (\nabla T') \rangle \leq 0$. However, scaling analysis suggests that $\langle T \rangle \sim \lambda^{-1}$ and $\langle T'D' \rangle \sim \lambda^{-2}$, where λ is the typical length scale of the studied process. Hence, for small-scale processes, diffusion can become of order one ($\text{Pe} \simeq 1$) or even leading order ($\text{Pe} > 1$). This means that at equilibrium (i.e., $\partial_t \langle \sigma_T'^2 \rangle = 0$), the small-scale dissipative term plays a role in the balance of the mean variance of the anomaly.

b. Restriction to a horizontal framework

Since we only have access to horizontal velocity (section 2), we restrict our study to horizontal interactions and adapt the general derivations of section 3a. First, we redefine T as the difference between the observed temperature and its horizontal global mean. With this definition, T is the departure from the mean at ~ 1000 m, showing regions warmer and colder than the mean and thus the spatial structure of the temperature at this depth. In this context, it is similar to the available potential energy (APE; Lorenz 1955), where for our reference depth, there are regions with higher and lower density (colder and warmer) and so higher and lower APE, respectively. For the impact of turbulent flow on the mean temperature, we have only $\mathcal{C}_{\text{hor}} = -\nabla_H^\dagger \cdot \overline{\mathbf{u}_H' T'}$, where

$\mathbf{u}_H^\dagger = (u, v)$ is the two-dimensional horizontal velocity vector, $\nabla_H^\dagger = (\partial_x, \partial_y)$ is the two-dimensional horizontal derivative operator, and $\cdot$ now represents the two-dimensional scalar product.

For the impact on the temperature variance within a horizontally restricted framework, we obtain

$$\mathcal{R}_{\text{hor}} = -2\overline{T} \nabla_H^\dagger \cdot \overline{\mathbf{u}_H' T'}, \quad (12a)$$

$$\mathcal{A}_{\text{hor}} = -2\nabla_H^\dagger \cdot (\overline{T \mathbf{u}_H' T'}), \quad (12b)$$

$$\mathcal{T}_{\text{hor}} = 2(\nabla_H \overline{T})^\dagger \cdot \overline{\mathbf{u}_H' T'}. \quad (12c)$$

Key properties of the eddy-mean interactions still remain even when focusing on the horizontal components, though. Hence, when globally averaged, the horizontal component of the nonlocal eddy-mean interaction component reads

$$\begin{aligned} \iint_S \mathcal{A}_{\text{hor}} ds &= -2 \iint_S \nabla_H^\dagger \cdot (\overline{\mathbf{u}_H' T' T'}) ds = -2 \oint_L (\mathbf{n}^\dagger \cdot \overline{\mathbf{u}_H' T'}) \overline{T'} dl \\ &\simeq 0, \end{aligned} \quad (13)$$

where S and L define the ocean surface and boundary at the studied depth, respectively, ds and dl define their surface and length elements, and $\mathbf{n}$ is the vector normal to the boundary. Hence, $\mathbf{n}^\dagger \cdot \overline{\mathbf{u}_H'}$ is the projection of the horizontal turbulent flow on the normal-boundary vector, which is close to 0 assuming a strong boundary slope and because of mass conservation (i.e., no mass is transported through the boundary). This means that, even when focusing on the horizontal component, the global average of the nonlocal component is still close to 0: there is weak net global eddy transport of residual temperature variance. As a consequence, the local and total components become almost equal:

$$\iint_S \mathcal{R}_{\text{hor}} ds \simeq \iint_S \mathcal{T}_{\text{hor}} ds. \quad (14)$$

Hence, even when focusing on the horizontal components, if assuming a strong boundary slope, loss and gain of mean variance are almost equivalent to gain and loss of eddy variance, allowing the unequivocal interpretation of total/local global-mean components as variance transfers. As a global average, this term is the forcing term of the spatial variance of the mean temperature field. It shows how the turbulent flux maintains or destroys, depending of the sign, the large-scale structure of the Conservative Temperature. Hence, it measures the ability of the turbulence to broaden or sharpen the Conservative Temperature distribution.

The reason for only focusing on the horizontal components of the transfers is a direct consequence of the dataset limitation. However, we can still estimate the relative error of this constraint. Colin de Verdière and Tailleux (2005) and Sévellec and Huck (2016) have suggested the existence of a dimensionless number (ϵ) that measures the ratio of the horizontal advection to the vertical one. It derives from the advection equation of neutral density under the assumptions of geostrophic and hydrostatic balances. This reads

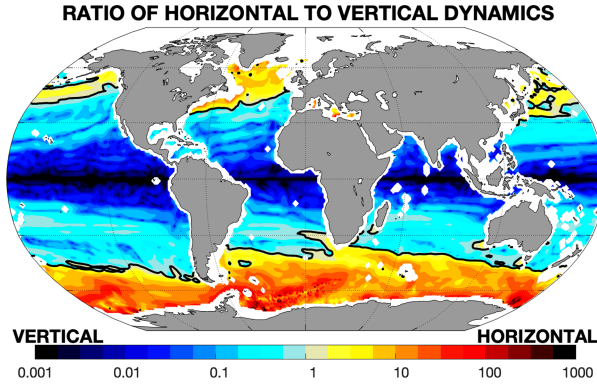


FIG. 4. Ratio of horizontal to vertical dynamics in log scale, following (15). The ratio (ϵ) measures the propensity of the advection equation to be dominated by horizontal advection ($\epsilon \gg 1$) or by vertical advection ($\epsilon \ll 1$) under the geostrophic balance assumption. The former regime is more inductive to baroclinic instabilities, whereas the latter regime is more inductive to baroclinic Rossby waves. The thick black contour corresponds to the perfect balance (i.e., $\epsilon = 1$).

$$\epsilon = \left| \frac{f}{h\beta} \frac{\|\nabla_H \gamma\|}{\partial_z \gamma} \right|, \quad (15)$$

where γ is the neutral density, f is the Coriolis parameter, $\beta = \partial_y f$ is the meridional variation of the Coriolis parameter due to Earth's curvature, $\|\nabla_H \gamma\| = \sqrt{(\nabla_H \gamma)^\dagger \cdot (\nabla_H \gamma)}$ is the neutral density horizontal gradient amplitude, and h is the pycnocline depth. The relative importance of horizontal and vertical advection has been reinterpreted by Sévellec and Huck (2015). They suggest the dominance of baroclinic instabilities in the horizontal “regime” ($\epsilon \gg 1$) and the dominance of baroclinic Rossby waves in the vertical regime ($\epsilon \ll 1$).

To estimate ϵ , we have used the ISAS17 product (Kolodziejczyk et al. 2023) which provides temperature and salinity gridded fields from an optimal interpolation (Bretherton et al. 1976; Gaillard et al. 2016) of Argo profiles. The neutral density was computed through the Gibbs SeaWater Oceanographic Toolbox of Thermodynamic Equation Of Seawater—2010 (TEOS-10) code. The estimation of the depth of the pycnocline was based on a scaling argument (i.e., typical depth of the pycnocline). Also, the studied turbulent processes are necessarily reaching the depth of the measurement. Hence, we set $h = 1000$ m.

Computing the dimensionless number ϵ (Fig. 4), we find that the horizontal regime is dominant poleward of the mid-latitudes (i.e., north of 35°N and south of 35°S). In particular, the ACC is largely in this horizontal regime, whereas the Gulf Stream and its eastward continuation as the North Atlantic Current, the Kuroshio, the Agulhas Current, and the Zapiola Gyre are marginally but still in this horizontal regime. On the other hand, subtropical and equatorial regions are in the vertical regime. (Note that the scaling is not informative at the equator because the geostrophic balance is invalid there.) As it will be shown later, this suggests that key regions for turbulent temperature flux, mean temperature gradient, and eddy-mean interactions are primarily within the horizontal regime.

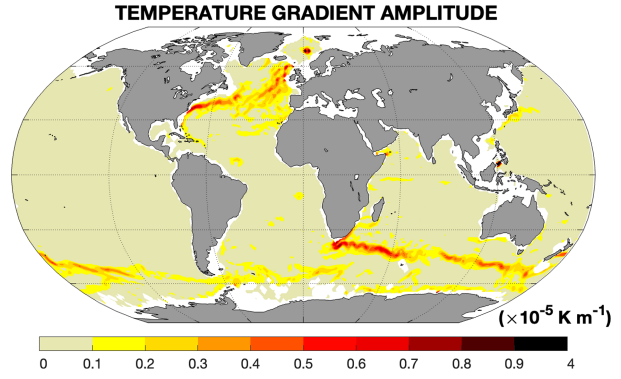


FIG. 5. Amplitude of the horizontal mean temperature gradient ($\|\nabla_H \bar{T}\|$).

Beyond this dynamical regime argument, it is worth noting that, in our framework, part of the temperature stratification has been included in a background reservoir (by removing $\langle \Theta \rangle_{\text{hor}}$). Hence, it is not acting, per se, within the temperature interaction terms, but as a background source for the mean temperature variance. This further limits the importance of vertical motion as it is restricted to $w \partial_z T$, instead of $w \partial_z \Theta$. The difference $(\partial_z \langle \Theta \rangle_{\text{hor}})$ is fully acknowledged in our framework and will be used later to estimate the optimal vertical velocity (see section 4d).

4. Results

a. Data properties

Based on the previous section, rather than focusing on zonal and meridional components, we define the turbulent temperature fluxes with respect to the Conservative Temperature horizontal gradient. Looking at the gradient amplitude ($\|\nabla_H \bar{T}\|$), we find that it is intense along intense currents (Fig. 5). We can identify the regions of western boundary currents, such as the Gulf Stream and the Kuroshio, as well as the ACC. An important temperature gradient is also visible in the eastern part of the North Atlantic. This is created by the Mediterranean Water as it spreads into the cooler North Atlantic. Averaged over our 2° cells, we find values of the mean temperature gradient on the order of several 10^{-6} K m^{-1} and up to $4 \times 10^{-5} \text{ K m}^{-1}$.

Based on this mean temperature gradient, we compute the turbulent flux along and across isotherms. This reads

$$\overline{u'_H T'}|_{\parallel} = \overline{u'_H T'} \times \frac{\nabla_H \bar{T}}{\|\nabla_H \bar{T}\|}, \quad (16a)$$

$$\overline{u'_H T'}|_{\perp} = \overline{u'_H T'}^\dagger \cdot \frac{\nabla_H \bar{T}}{\|\nabla_H \bar{T}\|}, \quad (16b)$$

where $\times$ is the two-dimensional vector product and $\parallel$ and $\perp$ denote the along- and across-isothermal directions, respectively. We find that both components are important (Fig. 6). This means that there are turbulent fluxes both across and along the mean temperature gradient. These fluxes reach values from a few to several $10^{-2} \text{ K m s}^{-1}$ with a maximum absolute value of 0.15 K m s^{-1} . Focusing on the along-isothermal component, we

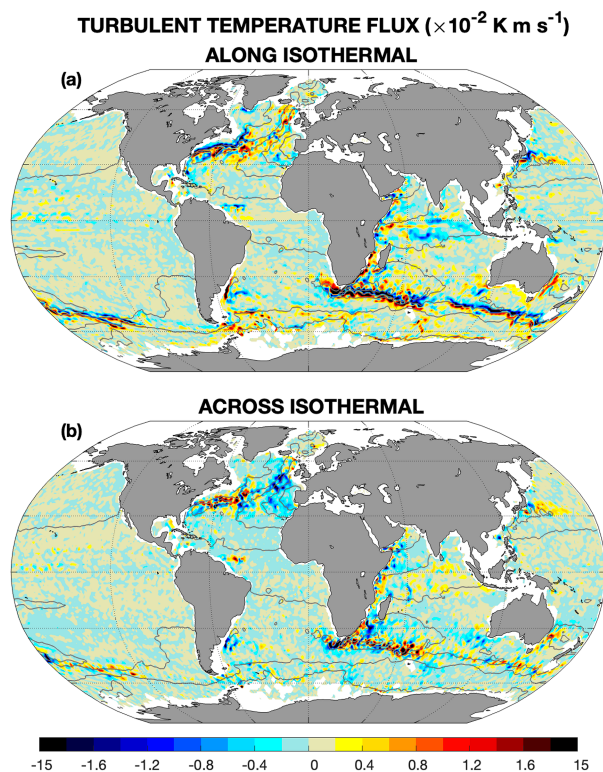


FIG. 6. Horizontal turbulent temperature flux. Flux projected (a) along conservative isotherms ($\overline{\mathbf{u}_H' T'}|_{\parallel}$) and (b) across conservative isotherms ($\overline{\mathbf{u}_H' T'}|_{\perp}$), following (16). Contours show mean Conservative Temperature with contours from -2° to 13°C with a 1.5° contour interval.

find consistent patterns that are elongated along isotherms. They are particularly strong along the Gulf Stream, the Kuroshio, and the ACC. For all three of these currents, the along-isothermal turbulent flux corresponds to a positive term to the south and a negative term to the north of the mean temperature gradient amplitude maximum (Fig. 5). Focusing on the across-isothermal component, while the most intense patterns are still in intense boundary currents and within the ACC, they also exist in the east North Atlantic (at the edge between the Mediterranean Water and the North Atlantic Deep Water). This region is quite consistently negative. Only 55% of the cross-isothermal turbulent temperature flux is Θ downgradient (i.e., $\overline{\mathbf{u}_H' T'}|_{\perp} < 0$). This suggests that a typical diffusivity closure (i.e., Fick's law, Redi 1982) will miss almost half of the fluxes if reconstructed by a downgradient flux of mean temperature. Note that this is potentially not problematic for the mean temperature evolution [i.e., $\mathcal{C}$ in (6)], as only the divergent part of the flux is key (appendix, Marshall and Shutts 1981; Fox-Kemper et al. 2003). Following the same principle, we find that only 46% of the cross-isopycnal turbulent temperature flux is γ -downgradient [i.e., $(\overline{\mathbf{u}_H' T'} \cdot \nabla_H \bar{\gamma}) / (\|\nabla_H \bar{\gamma}\|) < 0$, where γ is the neutral density]. Overall, turbulent fluxes appear strong within regions of intense currents.

To estimate the impact of the turbulent flux onto the mean temperature evolution, we compute its divergence

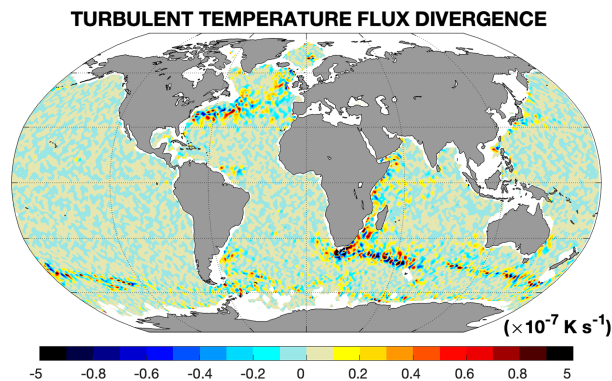


FIG. 7. Horizontal divergence of the horizontal turbulent temperature flux ($\mathcal{C}_{\text{hor}} = -\nabla_H^T \cdot \overline{\mathbf{u}_H' T'}$). This term corresponds to the horizontal components of the closure term (i.e., the impact of turbulence) for the mean temperature, following (6a).

(i.e., $\mathcal{C}_{\text{hor}} = -\nabla_H^T \cdot \overline{\mathbf{u}_H' T'}$). We find that the fluxes are on the order of several 10^{-8} K s^{-1} ($\sim 1 \text{ K}$ in 3 years), with a maximum absolute value of $5 \times 10^{-7} \text{ K s}^{-1}$ (Fig. 7). The divergence of the turbulent flux occurs mainly within intense boundary currents and shows a succession of positive and negative values corresponding to warming and cooling of the mean temperature by the turbulence, respectively. The typical spatial scale corresponds to consistent patterns of a few to several degrees.

To estimate regional impacts of the flux divergence, we compute its mean globally and over six active regions: the whole North Atlantic— 80°W – 0° and 25° – 60°N , the western North Atlantic— 80° – 46°W and 25° – 60°N , the central North Atlantic— 46° – 30°W and 25° – 60°N , the eastern North Atlantic— 30°W – 0° and 25° – 60°N , the Agulhas Current sector— 10° – 90°E and 55° – 20°S , and the Southern Ocean sector—south of 35°S (as shown in Fig. 2a). This shows that the regional effect depends on the region considered (Table 1). At the studied depth, globally the turbulence tends to warm the mean temperature by $3.9 \times 10^{-11} \text{ K s}^{-1}$ ($\sim 1 \text{ K}$ per millennium). This warming tendency is also true for the whole North Atlantic and its western subregion. The turbulence of the western North Atlantic leads to a warming of $\sim 1 \text{ K century}^{-1}$. It is the most intense average temperature changes that we have identified over the six tested regions. Indeed, the central North Atlantic is more neutral, with only a slight warming on average (100 times as low as the west North Atlantic). On the other hand, turbulence in the east North Atlantic, the Agulhas sector, and the Southern Ocean sector all tends to cool the mean temperature. It is the most intense in the Southern Ocean sector, with an average cooling of $\sim 1 \text{ K (150 yr)}^{-1}$.

b. Horizontal eddy–mean interactions

Now that the overall mean and turbulent states have been described, we focus on the three interaction terms: total, non-local (or variance redistribution), and local (or variance transfers), following (7) and their horizontal expression [(12)]. Our estimations suggest values on the order of a few $10^{-7} \text{ K}^2 \text{ m}^{-1}$ for the total and nonlocal terms and of several $10^{-8} \text{ K}^2 \text{ m}^{-1}$ for the local term (Fig. 8). We find that 88% of the ocean is

TABLE 1. Spatial averages of turbulent temperature flux divergence both at global and regional levels ($C|_{\text{hor}} = -\nabla_H^T \cdot \overline{\mathbf{u}_H' T'}$). The six regions (Fig. 2a) correspond to the whole North Atlantic (80°W–0° and 25°–60°N), the western North Atlantic (80°–46°W and 25°–60°N), the central North Atlantic (46°–30°W and 25°–60°N), the eastern North Atlantic (30°W–0° and 25°–60°N), the Agulhas Current sector (10°–90°E and 55°–20°S), and the Southern Ocean sector (south of 35°S). Consistently with (6a), positive and negative values correspond to positive and negative trends of the mean temperature, respectively.

$10^{-11} \text{ K s}^{-1}$	Global mean	North Atlantic				Agulhas Current	Southern Ocean
		All	West	Central	East		
Total	3.9	6.8	34.4	0.3	−15.5	−12.5	−21.2

dominated by the nonlocal term over the local one ($\mathcal{A}|_{\text{hor}}$ vs $T|_{\text{hor}}$). This is quite interesting as we know that on global scale, the redistribution vanishes. This result is consistent with the one for momentum transfer (i.e., kinetic energy) where similar dominance was found (Sévellec et al. 2025a). Looking at the residual [i.e., $\mathcal{R}|_{\text{hor}} - (\mathcal{A}|_{\text{hor}} + T|_{\text{hor}})$] as a proxy for the diagnostic error of the eddy–mean interactions, we find that this term remains small, even compared to the local term (Fig. 8d).

The regions of strong interactions are mainly associated with regions of strong temperature variance rather than of strong eddy kinetic energy (Fig. 2). They correspond to the North Atlantic along the Gulf Stream and its associated North Atlantic Current, the Agulhas Current, and, but more moderately, the ACC (Fig. 8). The total and nonlocal terms also have a signature along the east coast of Africa and along the

equator in the Indian Ocean (Figs. 8a,b). As expected from its expression ($T|_{\text{hor}} = 2\overline{\mathbf{u}_H' T'}|_{\perp} \|\nabla_H T\|$), the local term is the projection of turbulent flux onto the mean temperature gradient (Fig. 8c vs Figs. 5 and 6b). Here, the inconsistency between the observed turbulent flux and the downgradient closure becomes obvious and is potentially dramatic for temperature variance transfers. Indeed, the existence of $T|_{\text{hor}} > 0$ is directly related to the upgradient flux (regardless of the rotational term) and requires negative diffusivity coefficients for Fick’s law to be applied (appendix). Hence, at the $2^\circ \times 2^\circ$ scale and for the temperature variance budget, the observed variance transfers questions the validity of traditional downgradient flux turbulent closure (Redi 1982) and the use and estimations of positive diffusivity coefficients (e.g., Klocker and Abernathy 2014; Groeskamp et al. 2020; Roach et al. 2018; Sévellec et al. 2022).

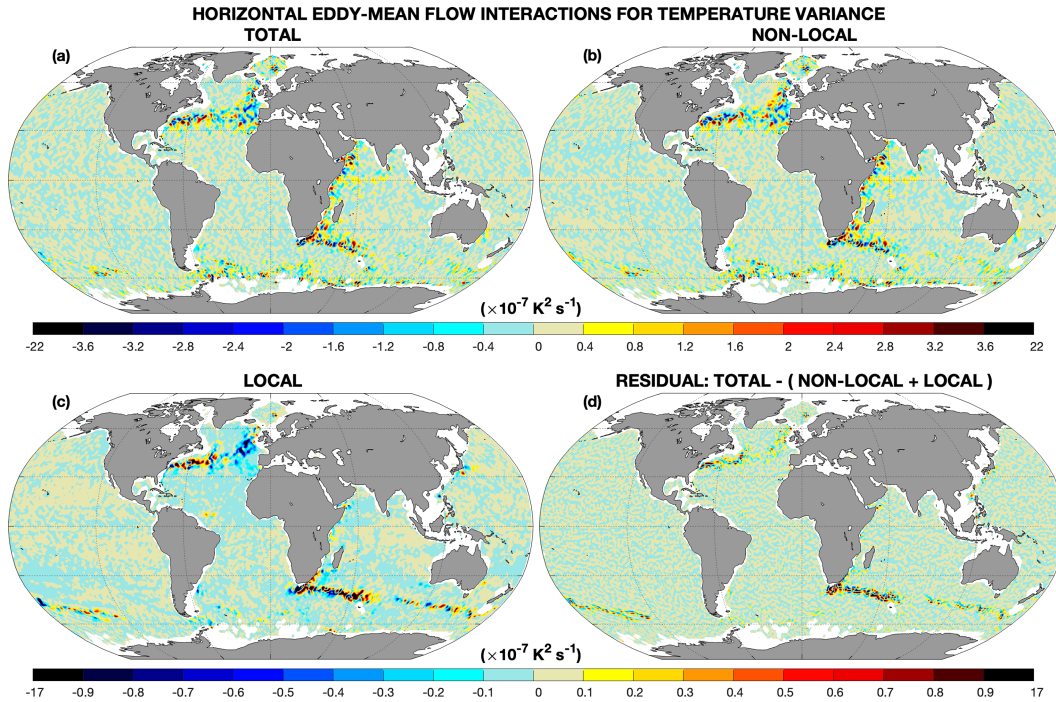


FIG. 8. Components of the horizontal eddy–mean interactions for the temperature variance: (a) total ($\mathcal{R}|_{\text{hor}}$), (b) nonlocal ($\mathcal{A}|_{\text{hor}}$), (c) local ($T|_{\text{hor}}$), and (d) residual ($\mathcal{R}|_{\text{hor}} - \mathcal{A}|_{\text{hor}} - T|_{\text{hor}}$), following (12). The residual should be equal to 0 and so measures the estimation error of the eddy–mean interactions. Note the different color scales for (a) and (b) vs (c) and (d). Positive and negative values correspond to variance transfers from ETV to MTV and from MTV to ETV, respectively.

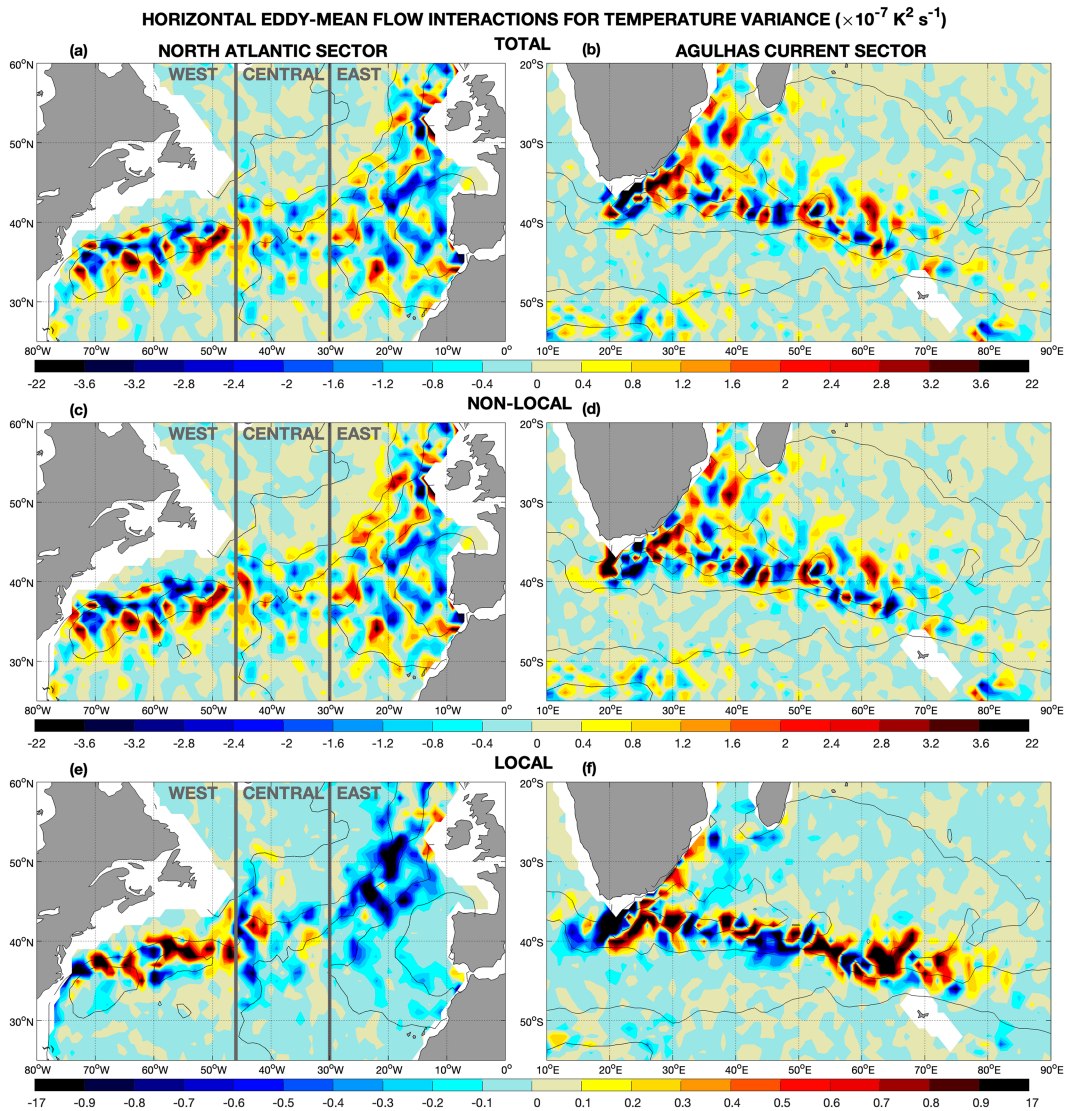


FIG. 9. As in Fig. 8, but zoomed for two key regions: (a),(c),(e) the west and east North Atlantic sectors and (b),(d),(f) the Agulhas Current sector. Components of the horizontal eddy-mean interactions for the temperature variance: (a),(b) total ($\mathcal{R}_{\text{hor}}$), (c),(d) nonlocal ($\mathcal{A}_{\text{hor}}$), and (e),(f) local ($\mathcal{T}_{\text{hor}}$), following (12). Positive and negative values correspond to variance transfers from ETV to MTV and from MTV to ETV, respectively. Contours show Conservative Temperature with contours from -2° to 13°C with a 1.5° contour interval.

Focusing on the two key regions, the North Atlantic and the Agulhas Current sector (as defined above), we see again that the nonlocal term is almost 4 times as large as the local one (Fig. 9). However, patterns are more spatially consistent for the local term than for the nonlocal term. Indeed, the total and nonlocal terms show positive and negative values of typical spatial scale of $\sim 5^\circ$, whereas the local term shows values which extend over almost $\sim 10^\circ$. In particular, in the eastern North Atlantic, the local term is almost exclusively negative, with the core of the pattern extending over $\sim 15^\circ$ in both longitudes and latitudes. This suggests a region of intense variance transfers from the mean temperature to the turbulent one. We hypothesize that this region of (mostly) downgradient thermal

turbulence is linked to “free” mesoscale turbulence (away from its formation in the Gulf Stream), consistent with (positive) trajectory dispersion (Taylor 1922; Batchelor 1949).

When globally averaged, the total interaction is negative with the expected dominance of the local term (Table 2). This suggests that variance is transferred from the mean to the turbulence. Looking at the six key regions (already defined above), the spatial averages reveal that most regions are prone to negative interaction (i.e., destruction of the mean temperature structure) except for the west North Atlantic (Table 2). In this region, the mean temperature structure is maintained, whereas the temperature turbulence is decreased. In the west North Atlantic, the Agulhas Current, and the Southern Ocean,

TABLE 2. Spatial averages of the horizontal variance transfers, following (12), both at global and regional levels. The six regions (Fig. 9) correspond to the whole North Atlantic (80°W–0° and 25°–60°N), the western North Atlantic (80°–46°W and 25°–60°N), the central North Atlantic (46°–30°W and 25°–60°N), the eastern North Atlantic (30°W–0° and 25°–60°N), the Agulhas Current sector (10°–90°E and 55°–20°S), and the Southern Ocean sector (south of 35°S). Positive and negative values correspond to variance transfers from ETV to MTV and from MTV to ETV, respectively. The residual reflects the error of the diagnostics.

$10^{-9} \text{ K}^2 \text{ s}^{-1}$	Global mean	North Atlantic				Agulhas Current	Southern Ocean
		All	West	Central	East		
Total	−0.5	−5.6	3.7	−5.5	−14.9	−0.4	−1.7
Nonlocal	0.2	0.2	1.9	−0.2	−1.1	1.4	−0.8
Local	−0.7	−6.0	1.8	−5.2	−14.3	−1.5	−0.8
Residual	0.0	0.2	0.0	−0.1	0.5	−0.3	−0.1

the variance redistribution remains as intense as the variance transfer. This is consistent with regions of intense current where advection plays a crucial role in redistributing variance. In all tested regions and globally, the residual term is weak, suggesting the robustness of the computed diagnostics.

c. Consequences for mean temperature distribution maintenance

Since T is the only term that has a global impact and, hence, any impact on the width of the mean temperature distribution, we focus on this term in the following subsection.

We decompose the global variance transfer in terms of temperature classes to determine how each class contributes to the overall shrinking of the mean temperature distribution. Following the water-mass transformation framework (Walín 1982), one can derive the variance transformations as a function of temperature classes. This reads

$$\Psi = \rho_0 C_p \partial_{\bar{T}} \iint_{S(\bar{\Theta}'' \leq \bar{\Theta})} T ds \Delta z, \quad (17)$$

where $S(\bar{\Theta}'' \leq \bar{\Theta})$ is the ocean surface at 1000 m with temperature lower than or equal to $\bar{\Theta}$, ρ_0 is the reference density, C_p is the ocean heat capacity, and Δz is an ocean-layer thickness. As discussed in Sévellec et al. (2025b), Δz should be set based on the increment of the temperature classes to make $\Psi^\#$ independent of this increment choice. At this depth, Sévellec et al. (2025b) suggest the use of $\Delta z|_{\text{ref}} = 70 \text{ m}$ for a neutral density increment of $\Delta \gamma|_{\text{ref}} = 0.03 \text{ kg m}^{-3}$. Hence, through a scaling, this corresponds to a thickness $\Delta z = \alpha \Delta T \Delta z|_{\text{ref}} / \Delta \gamma|_{\text{ref}} = 58.3 \text{ m}$ for our temperature increment of $\Delta T = 0.25 \text{ K}$ (and a spatial mean thermal expansion coefficient of $\alpha = 0.1 \text{ kg m}^{-3} \text{ K}^{-1}$).

This diagnostic reveals that for almost all the temperature classes, the variance transfers contributes to the shrinking of the mean temperature distribution (Fig. 10). This remarkable consistency contrasts with the intricate structure of the geographical distribution of the variance transfers (Fig. 8c). For a few water classes, however, the variance transfers lead to a broadening of the distribution. This is the case for extreme water classes: Conservative Temperature below 0.5°C and above 11.25°C (although this result has to be moderated since these temperature ranges correspond to poleward locations where there is the least amount of observations). It is also the case for Conservative Temperature between 6.5° and 7.25°C.

Overall, the variance transformation is not proportional to the volume of water; for instance, the AAIW has the largest volume, but this is not where the variance transformation maximum occurs. Basically, the volume distribution is sharper than the variance transformations. Also, there is a temperature-class lag in their distribution center with a peak at $\sim 4.5^\circ\text{C}$ and between 5° and 5.5°C for the former and the latter, respectively.

To describe the variance transformations as a function of water masses, we first defined seven main water masses located at 1000-m depth. These correspond to the AIW (from -1.50° to 3.00°C and $34.87\text{--}35.17 \text{ g kg}^{-1}$), the AABW (from -0.90° to 1.70°C and $34.81\text{--}34.89 \text{ g kg}^{-1}$), the CDW ($0.10^\circ\text{--}2.00^\circ\text{C}$ and $34.78\text{--}34.90 \text{ g kg}^{-1}$), the NADW ($1.50^\circ\text{--}4.00^\circ\text{C}$ and $34.97\text{--}35.17 \text{ g kg}^{-1}$), the AAIW ($2.01^\circ\text{--}10.00^\circ\text{C}$ and 33.96--

DISTR. OF HOR. LOCAL EDDY-MEAN FLOW INTER. (PW)

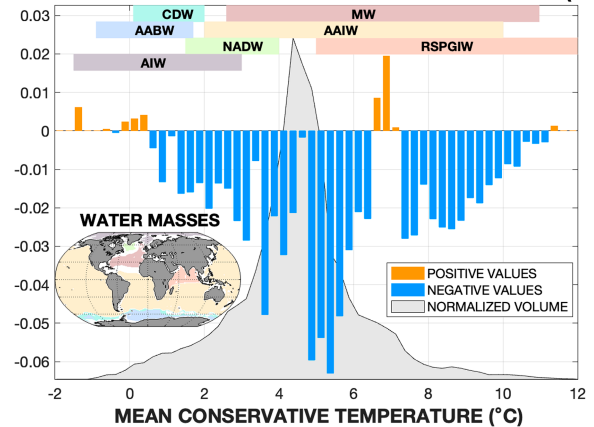


FIG. 10. As in Fig. 8c, but as a distribution in terms of Conservative Temperature classes, following (17). This corresponds to the distribution of local eddy-mean interactions for the temperature variance ($T|_{\text{hor}}$), following (12), as a function of the mean temperature. Positive (orange) and negative (cyan) values correspond to variance transfers from ETV to MTV and from MTV to ETV, respectively. The relative volume of each water class is given by the gray patch. Temperature classes are spaced by 0.25°C , and the volume curves have been smoothed using a 1°C moving average. The horizontal color patches show properties of selected water masses: AABW, CDW, AAIW, RSPGIW, MW, NADW, and the AIW, following Emery (2018). These water-mass locations are depicted in the inset.

34.97 g kg⁻¹), the MW (2.60°–10.97°C and 35.17–36.38 g kg⁻¹), and the RSPGIW (5.00°–13.98°C and 34.97–35.57 g kg⁻¹). The above Conservative Temperature and Absolute Salinity characteristics have been derived from Emery (2018) and positioned using both Conservative Temperature and Absolute Salinity from ISAS17 (inset of Fig. 10). This description allows for characterizing water masses with a positive variance transformation: the AIW, the AABW, the RSPGIW, and the mildest part of the MW (Fig. 10). On the other hand, the other water masses all correspond to an overall negative variance transfer of mean temperature variance. This sharpening of the temperature distribution is particularly active within the MW (Fig. 10).

d. Implications for mean temperature structure balance

Moving back to the global-mean temperature variance transfers, at high Péclet number and at equilibrium ($\partial_t \bar{T}^2 = 0$), from (10) we have $2\langle \bar{T}\bar{F} \rangle = -\langle T \rangle$. Assuming an optimal flux (i.e., perfect match with the temperature structure), we have $\bar{F}_{\text{opt}} = \mu(\bar{T}/\sigma_{\bar{T}})$ (where μ is a scalar), and we obtain $\mu = -(1/2)(\langle T \rangle/\sigma_{\bar{T}})$. Applying it to our horizontal framework, the minimum heat flux amplitude to balance the transfer terms is $\mu|_{\text{hor}} = 2.0 \times 10^{-10} \text{ K s}^{-1}$ or $4.7 \times 10^{-2} \text{ W m}^{-2}$ (after multiplying by $\rho_o C_p \Delta z$ to obtain an equivalent heat flux). This suggests that the minimal heat flux required to maintain the horizontal temperature structure at 1000 m given the action of the turbulence corresponds to a warming of $\sim 1 \text{ K}$ per 150 years.

Since this study focuses only on the horizontal component, the reference Conservative Temperature is a horizontal average (i.e., $\langle \Theta \rangle_{\text{hor}}$). Hence, a pseudovertical advection of the form $\bar{w}_z \langle \Theta \rangle_{\text{hor}}$ was incorporated to the mean temperature evolution equation as a forcing term, as explained in section 3a. At 1000-m depth, this should be the main term in the forcing term (i.e., $\bar{F}|_{\text{hor}}$). This allows for the computation of an optimal vertical velocity, following $\bar{F}_{\text{opt}}|_{\text{hor}} = -\bar{w}_{\text{opt}} \partial_z \langle \Theta \rangle_{\text{hor}}$ and using the expression of $\bar{F}_{\text{opt}}$ provided above. This reads

$$\bar{w}_{\text{opt}} = \frac{\bar{T}}{2\partial_z \langle \Theta \rangle_{\text{hor}}} \frac{\langle T|_{\text{hor}} \rangle_{\text{hor}}}{\sigma_{\bar{T}}^2|_{\text{hor}}}, \quad (18)$$

where $\sigma_{\bar{T}}^2|_{\text{hor}} = \langle \bar{T}^2 \rangle_{\text{hor}}$ is the horizontal variance of the mean temperature. This corresponds to a transfer from the reference state ($\langle \Theta \rangle_{\text{hor}}$) to the mean temperature structure ($\bar{T}^2$) by mean vertical motions ($\bar{w}$). This is equivalent to a transfer between the background potential energy and the available potential energy, in the context of potential energy transfers. (Note that, even at equilibrium, the equality linking variance transfers and forcing is only true on a global average, since locally advection can transport from local sources to local sinks.) Since the ANDRO database does not contain observations of vertical temperature shear, we computed it from the ISAS product (Kolodziejczyk et al. 2023). We find values of $\bar{w}_{\text{opt}}$ on the order of 10^{-7} m s^{-1} (Fig. 11), which corresponds to about a centimeter per day. These values are weaker and so consistent with mesoscale vertical velocity estimations of Christensen et al. (2024). As expected from the formulation of (18), the horizontal structure varies together with the mean

OPTIMAL EQUIVALENT VERTICAL VELOCITY ($\times 10^{-7} \text{ m s}^{-1}$)

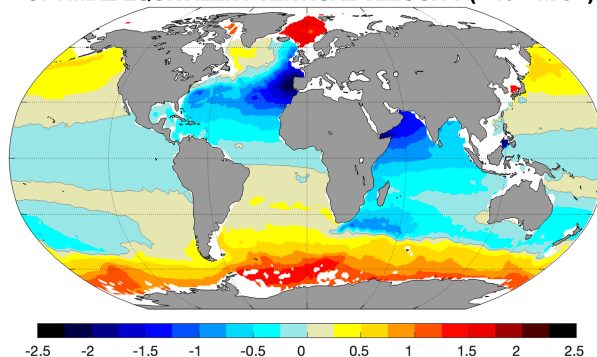


FIG. 11. Optimal equivalent vertical velocity, following (18). This vertical velocity leads to the most efficient mean vertical advection allowing for a global compensation of the variance transfer (T). (Note that, even at equilibrium, there is no need for a perfect local compensation, since advection can transport variance from local sources to local sinks.) Gray contour shows Conservative Temperature of $\langle \Theta \rangle_{\text{hor}} \simeq 4.36^\circ\text{C}$ and perfectly matches $\bar{w}_{\text{opt}} = 0$ by construction of the anomalous Conservative Temperature (i.e., $T = \Theta - \langle \Theta \rangle_{\text{hor}}$).

temperature. This leads to upwelling of the colder waters: AABW, CDW, NADW, and AIW and downwelling of MW and RSPGIW (as well as of its residual within the recirculation of the Agulhas Current); the AAIW is both upwelled and downwelled depending if it is below or above a Conservative Temperature of $\langle \Theta \rangle_{\text{hor}} \simeq 4.36^\circ\text{C}$ (this threshold is an obvious consequence of the definition of $T = \Theta - \langle \Theta \rangle_{\text{hor}}$). Maximum upwelling occurs in the Nordic seas, whereas downwelling occurs off the Portugal coast.

Comparison with the actual vertical velocity at 1000-m depth (w_{real}) should be done carefully. Indeed, the optimal vertical velocity is the minimum vertical velocity needed to balance the temperature variance transfers, so it does not have to exactly reflect the real velocity. Hence, the actual vertical velocity only needs to contain the optimal velocity for consistency. Liang et al. (2017) and Cortés-Morales and Lazar (2024) have provided estimations of the vertical velocity, and in particular at 1000-m depth. It corresponds to a flow of a few to several 10^{-6} m s^{-1} . This is, at least, one order of magnitude above the required optimal velocity. At this depth, the retrieved estimated vertical velocity pattern bears a resemblance to the Ekman (1905) pumping pattern (Marshall and Plumb 2007; Wunsch 2011; Roquet et al. 2011). Hence, w_{real} corresponds to upwelling in the subpolar regions and downwelling in the poleward part of subtropical regions (north of 30°N and south of 30°S for the Northern and Southern Hemisphere, respectively). This is overall quite consistent with our optimal vertical velocity (Fig. 11). In particular, positive values in the subpolar North Atlantic and North Pacific, positive values in the Southern Ocean, negative values along the North Atlantic Current and within the Mediterranean Water, and negative values within the Agulhas Current, its retroflection, and its merging with the ACC are all consistent signatures of both w_{real} and w_{opt} . This suggests the positive projection of w_{opt} onto w_{real} and that w_{opt} can indeed be contained within w_{real} . Hence, even if not a perfect validation of w_{opt} ,

we can conclude that independent estimations of w_{real} are consistent with our framework and results. This suggests that the observed mean upwelling has the potential to balance the variance transfers estimated in the present study.

5. Discussion

In this study, we have developed a consistent framework to track and assess the eddy–mean interactions of temperature variance. To this purpose, we have built on analyses of variance budgets (e.g., Sévellec et al. 2006; Buckley et al. 2012; Sévellec et al. 2021) and of kinetic energy interactions (e.g., Chen et al. 2014, 2016; Sévellec et al. 2025a) to disentangle the temperature variance exchanges between the mean and the turbulence. This framework has some analogy with studies looking at potential energy exchanges (e.g., Kang and Curchitser 2015; Chen et al. 2016; Jamet et al. 2024). We find that the eddy–mean interactions are well described using three reservoirs: the mean temperature variance, the residual temperature variance, and the eddy temperature variance (Fig. 3). They correspond to the zeroth-, first-, and second-order terms of the temperature square, respectively. The RTV is peculiar in the sense that it is zero on average, but it is key in the sense that it acts as a mediator between MTV and ETV. In this context, we have shown that the total interactions are the sum of the nonlocal and local interactions, where the former corresponds to a temperature variance redistribution and the latter corresponds to temperature variance transfers.

To compute the temperature variance interactions, we have used consistent in situ global observations of temperature and horizontal velocity provided by the ANDRO dataset (Ollitrault and Rannou 2013). The ANDRO dataset is based on deep Argo float displacements, limiting our study to 1000-m depth. We find that the across-isothermal turbulent temperature fluxes are only 55% downgradient, challenging the applicability of downgradient flux closure (Redi 1982) to accurately represent temperature variance transfers. Regarding the temperature variance interactions, the pattern shows intensification in the Gulf Stream, in the North Atlantic Current, in the Agulhas retroflection, and in both ACC of the Indian Ocean sector and the Pacific Ocean sector. The typical length scale signature varies from several degrees to around a dozen of degrees. At the scale of the computation (i.e., $2^\circ \times 2^\circ$), the nonlocal terms are more intense than the local terms, leading to their dominance over the total interactions.

When averaged over a larger area, in almost all tested regions and in the global average, the variance transfers (i.e., local term $-T$) are negative and are the dominant term for the eddy–mean interactions (i.e., total term $-R$). This suggests a shrinking of the mean temperature distribution [restoring toward the mean value, consistently with the intuitive description of Zika et al. (2012)] and an intensification of turbulent activity. This view is also correct when looking at the average effect over mean temperature classes, where most of them correspond to a shrinking of the mean temperature distribution. This suggests that, unlike for the $2^\circ \times 2^\circ$ scale, the downgradient flux closure can represent accurately water-mass variance transformation. In contrast, the western North Atlantic is the only tested region where the turbulence acts to broaden the mean temperature distribution, whereas turbulent

activity is damped. Hence, this region acts as a graveyard for turbulence allowing the maintenance of mean temperature structure, hence of the mean circulation. Extrapolating this result to the full water column, this is consistent with this particular region being a warm region ($\overline{T} > 0$) where the ocean releases heat to the atmosphere ($\overline{F} < 0$; Tomita et al. 2021, for instance), and so having a negative correlation between heat flux and anomalous temperature field ($\overline{TF} < 0$). This leads to a mean temperature damping effect by the heat flux ($\partial_t \overline{T}^2 < 0$), which needs to be maintained by turbulent processes ($T > 0$). This is also supported by the relatively important positive contribution of the variance redistribution (i.e., nonlocal term $-A$) which also compensates the action of the heat flux and contributes to the maintenance of the mean temperature structure of this region.

Even if our study is only centered around the 1000-m depth, the properties of the interactions give us a unique observational insight into the dynamics of the ocean. Indeed, generalizing our results that the global-mean variance transfers are negative ($\langle T \rangle < 0$) has implications for ocean equilibrium. To this purpose, we first need to acknowledge a few properties: The large-scale dissipation term is negligible (i.e., high Péclet number: $\langle \overline{TD} \rangle \simeq 0$), the small-scale dissipation is of leading order and negative (as demonstrated in this study: $\langle \overline{T'D'} \rangle \leq 0$), the large-scale forcing is positive (i.e., warming in warm areas and cooling in cold areas: $\langle \overline{TF} \rangle > 0$), and we can hypothesize that the small-scale forcing, if it exists, is negative (i.e., warm and cold eddies transfer their properties to the atmosphere: $\langle \overline{T'F'} \rangle \leq 0$). This leads to the conclusion that, at equilibrium and globally, the mean large-scale forcing is either reinjected to the atmosphere as small-scale forcing or is transferred toward turbulent small-scale ocean dissipation:

$$\begin{aligned} 2\langle \overline{TF} \rangle &\rightarrow \sigma_T^2 \xrightarrow{\tau} \langle \sigma_{T'}^2 \rangle \xrightarrow{2\langle \overline{T'F'} \rangle} \frac{2\langle \overline{T'F'} \rangle}{2\langle \overline{T'D'} \rangle}. \end{aligned}$$

This is a (partial) observational evidence of the direct cascade of temperature variance, already established in an idealized configuration modeling study (Hochet et al. 2020), similar to the expected direct cascade of potential energy (Rhines 1977; Salmon 1978, 1980). This means that the large-scale forcing broadens the large-scale distribution which is balanced by a shrinking effect of variance transfers toward small-scale variance. This small-scale variance increase is balanced by small-scale dissipation or possibly a net anticorrelation of small-scale forcing and small-scale temperature anomaly. Hence, our study opens the possibility of rationalizing the ocean as a “device” converting large-scale forcing from the atmosphere to small-scale forcing to the atmosphere (Small et al. 2008) with some efficiency (i.e., small-scale ocean dissipation). Determining the relative effect of small-scale forcing and small-scale dissipation will be the goal of future analyses.

One consequence of our framework consistent with our limited dataset (i.e., a single slice of the ocean at 1000-m depth) is the need to define a background mean temperature gradient ($\partial_z \langle \Theta \rangle$). This background provides a source of variance through vertical motion impacting the mean temperature variance. This has allowed us to estimate an optimal vertical velocity needed to compensate the transfers toward the eddy

variance, which corresponds to only a few centimeters per day. Whereas the abyssal recipes allows for an estimation of the required turbulence based on observed circulation (Munk and Wunsch 1998), here we have used turbulence observations to estimate the required vertical velocity. This background $(\langle \Theta \rangle_{\text{hor}})$ bears an obvious resemblance with the reference state used to define the background potential energy (Lorenz 1955; Hochet et al. 2022), whereas the MTV and ETV ($\overline{T}^2$ and T'^2) are analogous to the mean and eddy available potential energy (Lorenz 1955; Hochet et al. 2022), respectively. Building on this relation might help define the background temperature, central to our study, in a robust, physically meaningful, and elegant manner.

Our study, being at a single depth, it obviously suffers from a limited view. Building a full three-dimensional picture based on observations of the eddy–mean interactions of temperature, salinity, and density variance will be the goal of future investigations. Beyond observations, testing our framework and results in long climate simulations which include eddy-resolving ocean models is a direction for future work. Indeed our study provides an observational estimate that can help test and validate eddy-resolving ocean numerical simulations. It also represents a step forward for the further development and implementation of ocean turbulent closures in laminar ocean numerical models.

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Data availability statement. The ANDRO dataset used in this study corresponds to the 2025 Release (key: “116520”) and is available at <https://doi.org/10.17882/47077>. The ISAS17 dataset provides a global three-dimensional gridded temperature and salinity data derived from objective analysis of in situ observations and is available at <https://doi.org/10.17882/52367>.

APPENDIX

Physical Interpretation of the Eddy–Mean Interactions

In this appendix, we derived the turbulent heat flux as well as the total, local, and nonlocal interactions following

two classical frameworks. This provides physical interpretations of the eddy–mean interaction terms.

a. Rotational and divergent decomposition

Following the Helmholtz decomposition, Marshall and Shutts (1981) and Fox-Kemper et al. (2003) suggested that the turbulent heat flux can be decomposed into a divergent and a rotational component. This reads

$$\overline{\mathbf{u}'T'}|_{\text{div}} = \nabla \phi, \quad (\text{A1a})$$

$$\overline{\mathbf{u}'T'}|_{\text{rot}} = \nabla \times \mathbf{A}, \quad (\text{A1b})$$

where ϕ is a scalar potential and $\mathbf{A}$ is a vector potential. [Note that ϕ and $\mathbf{A}$ are not uniquely defined (Fox-Kemper et al. 2003), leading, in practice, to the indeterminacy decomposition]. This framework leads to a simplification of the flux divergence acting on the mean temperature, as indicated in (6a):

$$\nabla^\dagger \cdot \overline{\mathbf{u}'T'}|_{\text{div}} = \nabla^2 \phi, \quad (\text{A2a})$$

$$\nabla^\dagger \cdot \overline{\mathbf{u}'T'}|_{\text{rot}} = 0, \quad (\text{A2b})$$

where ∇^2 is the Laplacian ($= \nabla^\dagger \cdot \nabla = \partial_x^2 + \partial_y^2 + \partial_z^2$). This implies that only the divergent term is important for the mean temperature evolution (Marshall and Shutts 1981). Equation (A2) is now routinely applied in oceanographic studies (e.g., Aoki et al. 2013; Guo and Bishop 2022). It potentially solves the apparent paradox of the important (45%) upgradient turbulent heat fluxes: part of them can come from the rotational term.

For the variance transfers [i.e., local interactions: $\mathcal{T} = 2(\nabla \overline{T})^\dagger \cdot \overline{\mathbf{u}'T'}$], both divergent and rotational components are potentially important. However, we have

$$(\nabla \overline{T})^\dagger \cdot \overline{\mathbf{u}'T'}|_{\text{rot}} = \nabla^\dagger \cdot (\overline{T} \mathbf{u}'T')|_{\text{rot}}. \quad (\text{A3})$$

Hence, assuming no net variance flux at the boundaries, we know that

$$\iiint_V (\nabla \overline{T})^\dagger \cdot \overline{\mathbf{u}'T'}|_{\text{rot}} dv = 0. \quad (\text{A4})$$

This means that the rotational component does not contribute to a net global temperature variance transfer.

We can conclude that, at the computational scale, both divergent and rotational components will be at play for the transfers and that the upgradient and downgradient properties of the turbulent heat flux select the direction of the transfers (i.e., toward the mean and toward the eddy, respectively). However, at global scale, only the divergent component contributes. We hypothesize that there exists a spatial scale over which the rotational component of the transfers vanishes. Under this assumption, a downgradient closure of the divergent component is consistent with our observations of negative transfers at global scale and for most tested spatial and water-mass averages (Table 2 and Fig. 10). Whereas this downgradient closure would be valid at all scales for the mean temperature evolution,

it would only be valid over this hypothesized spatial scale for variance transfers.

b. Symmetric and antisymmetric decomposition

Here, we follow another classical theoretical framework, namely, the temporal-residual-mean (McDougall and McIntosh 2001). This framework shows that the turbulent temperature flux can be represented through the mean temperature gradient. This reads

$$\overline{\mathbf{u}T'} \sim -(\mathbf{A} + \mathbf{S}) \cdot \nabla \overline{T}, \quad (\text{A5})$$

where $\mathbf{A}$ and $\mathbf{S}$ are antisymmetric and symmetric tensors, respectively. They represent rotation and deformation associated with eddy advection and diffusion closure, respectively.

Applying it to the total, local, and nonlocal interaction terms, following (7), we have

$$\mathcal{R} = -2\overline{T}\nabla^\dagger \cdot \overline{\mathbf{u}T'} \sim \nabla^\dagger \cdot [(\mathbf{A} + \mathbf{S}) \cdot \nabla \overline{T}^2] - 2(\nabla \overline{T})^\dagger \cdot \mathbf{S} \cdot \nabla \overline{T}, \quad (\text{A6a})$$

$$\mathcal{A} = -2\nabla^\dagger \cdot (\overline{T}\mathbf{u}T') \sim \nabla^\dagger \cdot [(\mathbf{A} + \mathbf{S}) \cdot \nabla \overline{T}^2], \quad (\text{A6b})$$

$$\mathcal{T} = 2(\nabla \overline{T})^\dagger \cdot \overline{\mathbf{u}T'} \sim -2(\nabla \overline{T})^\dagger \cdot \mathbf{S} \cdot \nabla \overline{T}. \quad (\text{A6c})$$

These formulations help us reinterpret the local and nonlocal terms. The nonlocal term corresponds to the eddy advection and eddy diffusion of mean temperature variance (exhibiting the action of both antisymmetric and symmetric tensors). They correspond to a spatial redistribution of variance (i.e., conserving the global mean variance). With this formulation, the residual temperature variance appears less useful as the mean temperature variance is self-consistent [as expected for the temporal-residual-mean framework; McDougall and McIntosh (2001)]. At the opposite, the local term is only controlled by the symmetric tensor. Also, its global integral does not vanish. This implies the possibility of a net global variance transfer between mean and eddy temperature variance. Consequently, and as mentioned in McDougall and McIntosh (2001) for density, only the symmetric component acts on the eddy temperature variance.

To further characterize the physical constraint behind the local term, we can split the symmetric tensor through an eigen-decomposition. The local term becomes

$$(\nabla \overline{T})^\dagger \cdot \mathbf{S} \cdot \nabla \overline{T} = \sum_{i=1}^3 \kappa_i (\mathbf{s}_i^\dagger \cdot \nabla \overline{T})^2, \quad (\text{A7})$$

where κ_i are the three diffusivity coefficients along the three natural directions $\mathbf{s}_i$, such as $\mathbf{S} = \sum_{i=1}^3 \kappa_i \mathbf{s}_i \cdot \mathbf{s}_i^\dagger$ (i.e., an eigen-decomposition of $\mathbf{S}$). Hence, $\mathcal{T} > 0$ can only come from a negative diffusivity coefficient (κ_i), reminiscent of the negative viscosity of Starr (1968).

This formulation suggests that, beyond the existence of rotational fluxes, the existence of $\mathcal{T} > 0$ (Fig. 8c) is inconsistent with Fick's law closure. Only when averaged over large spatial scales or water masses does this downgradient flux closure appear consistent with our observations (Table 2 and

Fig. 10, respectively), except for a few peculiar regions or water classes. It is worth noting that state-of-the-art direct and indirect estimations often lead, sometimes by construction, to positive-definite diffusivity coefficients (e.g., Klocker and Abernathy 2014; Groeskamp et al. 2020; Roach et al. 2018; Sévellec et al. 2022). This has the inherent consequence of restricting variance transfers from the mean to the eddy.

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