

# Decadal Oscillations in a Simplified Coupled Model due to Unstable Interactions Between Zonal Winds and Ocean Gyres

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## Abstract

Decadal oscillations are obtained in a simple coupled model, consisting in a one-layer bidimensional ocean model and a one-layer unidimensional energy-balance atmospheric model, including a parameterization of the zonal winds 'à la' Green, interacting through heat and momentum fluxes. The range of parameters leading to oscillations is determined through several numerical experiments: ocean eddy-diffusion smaller than estimations from observations is required for oscillations to be sustained. The essential physical processes are clarified, but the spatial pattern of the oscillation remains too complex for a simple low-order conceptual mechanism to emerge.

## Motivation

- Decadal variability is found in surface observations in the North Pacific Atlantic (Sutton and Allen 1997, Mann *et al.* 1998), and the subduct propagation of mid-latitude surface anomalies may influence tropical like ENSO (Gu and Philander 1997).
- Coupled climate models show variability in the North Pacific due to interactions between the subtropical gyre circulation and the Aleutian (Latif and Barnett 1994).
- Cessi (2000) and Gallego and Cessi (2000) exhibit a simple coupled conservation principles, that produce decadal oscillations due to the gyres heat transport and wind-stress, the key element being the delay circulation to changes in the wind-stress.

## The diagnostic atmospheric model

- zonally-averaged one layer of fixed height  $D$ , with constant stratification between horizontal eddy diffusion, incoming shortwave, outgoing longwave
- surface temperature  $\theta(y)$  determined through heat balance:

$$-C_{pa}\rho_a k_s d_e \partial_y^2 \theta = Q_{\text{SWA}} - (A + B\theta) - r[Q_{\text{SWO}} + \lambda(\theta - \theta_s)]$$

- zonal wind  $\tau(y)$  determined through momentum balance:

$$\tau - \frac{d_e k_s}{\gamma} \partial_y^2 \tau = -\frac{\rho_a k_s d_e}{d} \left[ \beta d + \frac{f}{S} (\partial_y \theta + L_\rho^2 \partial_y^3 \theta) \right]$$

where  $\int_0^{L_y} \tau dy = 0$  is used to determine the vertical eddy diffusion scale  $d$

$$\text{effective scale height } d_e = \frac{dD}{d+D} \quad (\sim 3600 \text{ m})$$

$$\text{baroclinic radius of deformation } L_\rho = \left( \frac{d d_e g S}{f^2 \Theta} \right)^{1/2} \quad (\sim$$

## The prognostic ocean model

- one “thermocline” layer of fixed depth  $H$  with wind-driven dynamics
- vertically homogeneous temperature  $T(x, y)$  integrated through heat b

$$C_{pw}\rho_w [H\partial_t T + J(\Psi, T)] = Q_{\text{SWO}} + \lambda(\theta - T) + C_{pw}\rho_w \nabla$$

- horizontal streamfunction  $\Psi(x, y)$  integrated from large-scale limit of q
- barotropic vorticity equation:

$$\partial_t \Psi - \beta R^2 \partial_x \Psi = \frac{R^2}{\rho_w} \partial_y \tau + \nabla \cdot (A \nabla \Psi)$$

where  $R$  is the Rossby radius of deformation (first baroclinic mode),

$K$  and  $A$  are the eddy diffusion coefficients for temperature and momentum

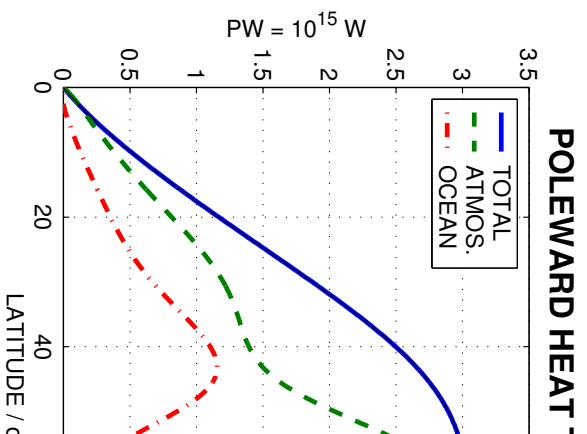
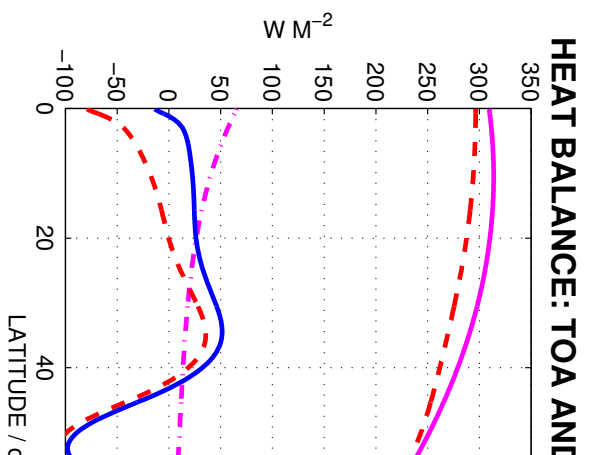
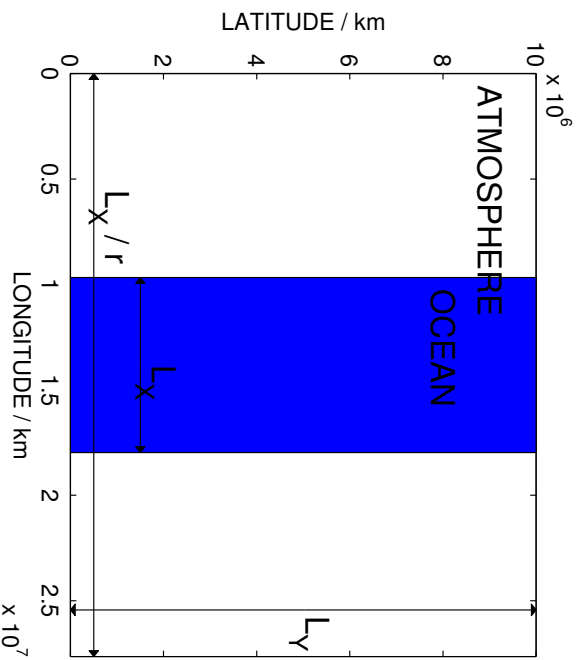
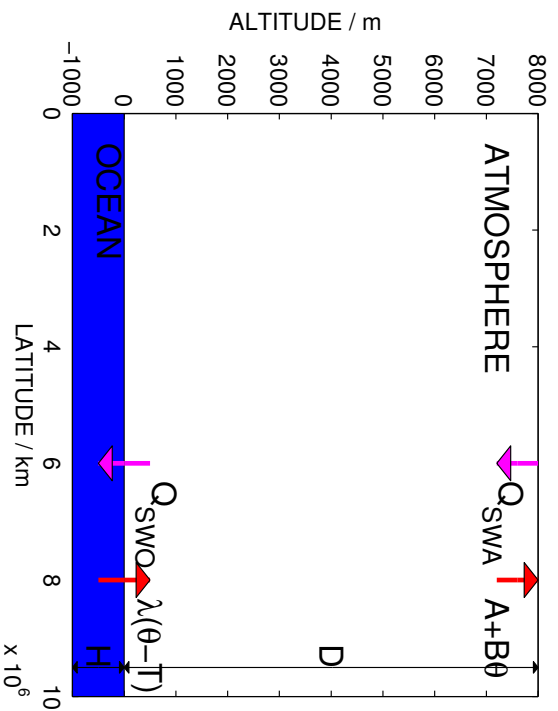
$\text{Coupling through surface heat flux } Q(x, y) = Q_{\text{SWO}}(y) + \lambda(\theta(y) - T(x,$
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## Configuration and parameters

- Cartesian coordinates single-hemisphere  $\beta$ -plane
- atmosphere of terrestrial width at  $45^\circ\text{N}$  (28000 km), ocean of North 1 both extending from Equator to Pole

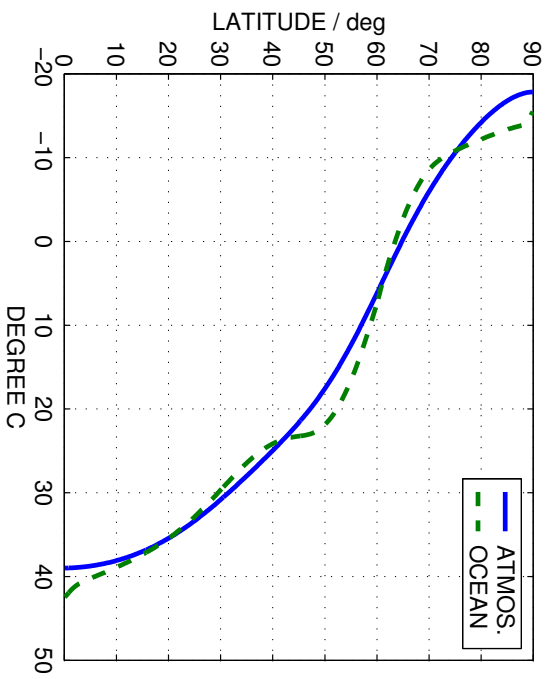
The only external forcing is the prescribed incoming solar radiation at the top and at the ocean surface. In spite of the simplicity and crudeness of the model, it is relatively well represented with trade winds in the tropics, westerlies in the mid-latitudes and easterlies poleward of  $80^\circ\text{N}$ .

Relatively low eddy-diffusivity is used in the ocean ( $K = A = 200 \text{ m}^2 \text{ s}^{-1}$ ) sustained. However a proper representation of the frictional western boundary layer is not possible. Viscosity in the zonal direction ( $2000 \text{ m}^2 \text{ s}^{-1}$ ), what is not necessary in current observations.

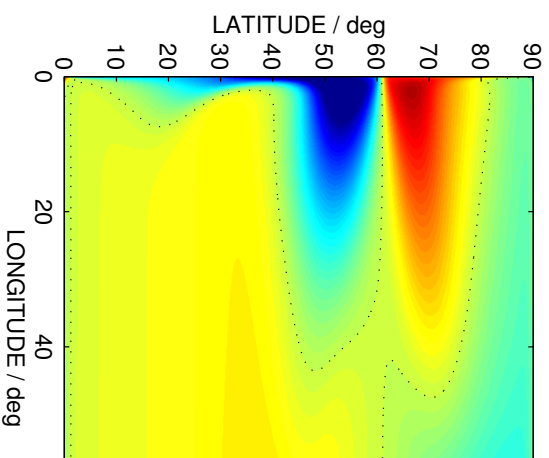


# The mean state

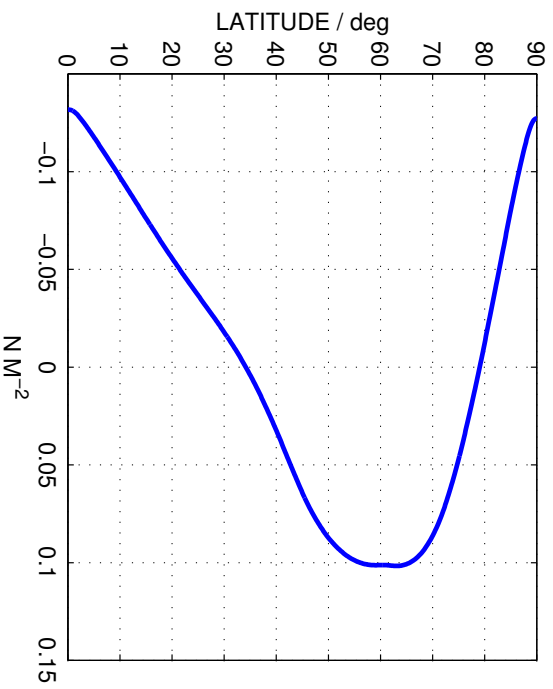
## ATMOSPHERIC SURFACE TEMPERATURE



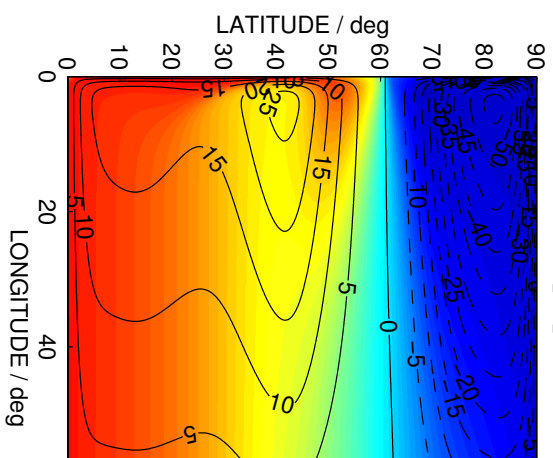
## OCEAN SURFACE HEAT FLUX



## ZONAL WIND STRESS



## OCEAN TEMPERATURE [C] & STRESS



## **Decadal oscillations**

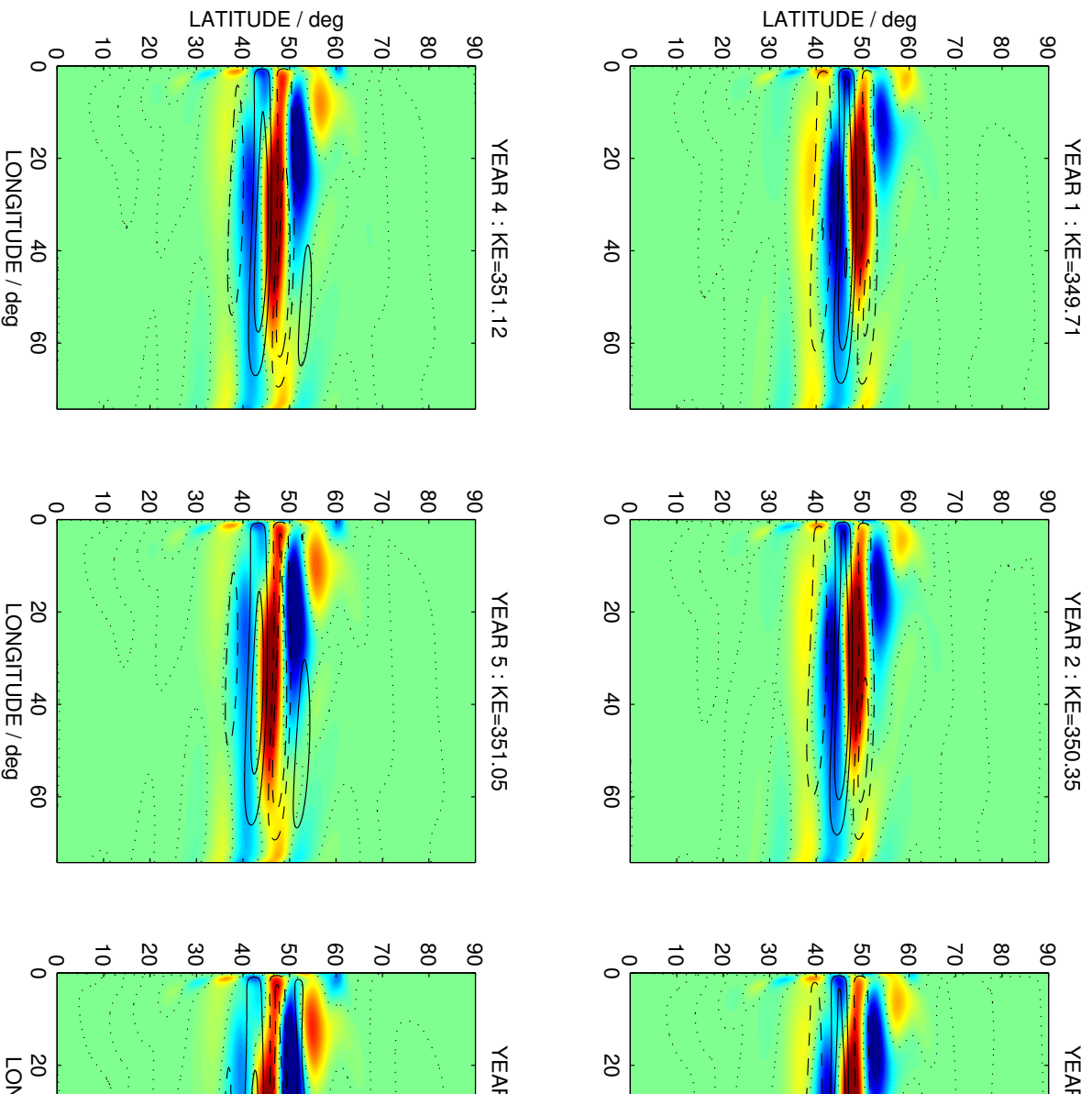
For a limited range of parameters, consisting in low atmospheric and ocean oscillations settle in place of a steady state. Periods are typically in the range 10-20 years. Temperature anomalies reach several degrees C in the ocean, but hardly 1 degree C in the atmosphere.

The variability is located south of the intergyre boundary, between 30°N and 30°S. The position of the zero wind-stress curl line remains stationary.

The anomalies structure is complex with a high meridional wavenumber. The anomalies are initiated at the separation point of the western boundary current, just east of the equator. Then, they extend easterly and move slowly southward. They die off after 2-3 years into the boundary current, almost 2 periods after their formation. The decadal variables follow the ocean anomalies along their meridional course.

However, the development of a positive SST anomaly at the western boundary is coincident with a minimum of the subtropical gyre intensity, because at the same time a streamfunction anomaly is of positive sign south of the zero wind stress curl line.





Anomalies of ocean temperature (blue: $-2^{\circ}\text{C}$ , red: $+2^{\circ}\text{C}$ ) and streamfunction (solid  $\geq 0$ , dashed  $< 0$ ) every year over half an oscillation period.

## The oscillation period

In this experiment, the oscillation period  $T = 12.5$  yr is easily related to the baroclinic Rossby waves across the basin:

$$\frac{L_X}{\beta R^2} = \frac{8000 \text{ km}}{1.6 \times 10^{-11} \text{ m}^{-1} \text{ s}^{-1} (35 \text{ km})^2} = 12.9 \text{ yr}$$

However Cessi (2000) shows that it is not that simple since the advection well. Indeed the same experiment with a slightly different boundary condition generate oscillations with a period of 19.5 yr.

Comparison of experiments with various parameters and boundary conditions determine exactly how the oscillation period is established.

## The oscillation mechanism

**Response of the wind stress  $\tau'$  to temperature anomalies  $\theta'$**

For large scale perturbations ( $l \gg L_\rho$  and  $l \gg L_d$ ,  $L_d = (d_e k_s / \gamma)^{1/2} \sim 55$

$$\tau' \propto -\frac{\rho_a f d_e k_s}{d S} \partial_y \theta'$$

**For small scale harmonic perturbations ( $l \ll L_\rho$  and  $l \ll L_d$ ):**

$$\tau' \propto \frac{\gamma \rho_a f L_\rho^2}{d S} \partial_y \theta' \propto \frac{\gamma g \rho_a d_e}{f \Theta} \partial_y \theta$$

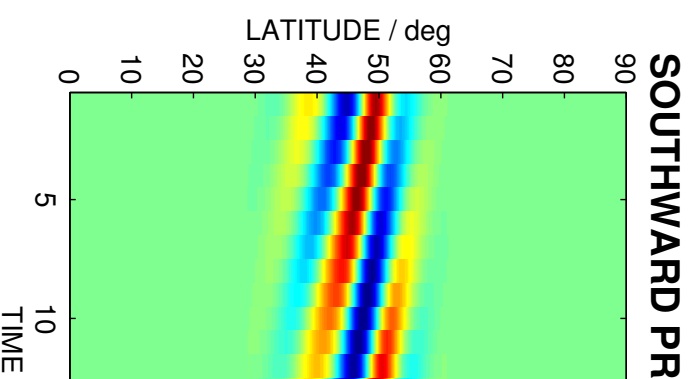
Note the opposite sign, but rather similar coefficient in amplitude (2.2 ×

### Propagation of temperature anomalies

Southward propagation of ocean temperature anomalies from 60°N to 30°N follows a passive advection by the mean flow, with a mean velocity of  $2.6 \times 10^{-3} \text{ m s}^{-1}$ .

### Remaining questions:

- what sets the meridional wavenumber?
- what is exactly the instability mechanism?



# Discussion

## Differences with Cessi (2000)

- boundary condition for wind speed at  $y = 0$  and  $y = L_y$ :  $\partial_y \tau = 0$  (instead of  $\tau = 0$ )
- several resolutions and parameters have been experimented and compared with the previous ones
- resolution and numerics do influence the occurrence of oscillations
- a numerical experiment with isotropic viscosity is now running ( $A_x = A_y = 10^{-10} \text{ m}^2 \text{ s}^{-1}$ )

## The paradox

It appears that the parameter range leading to oscillations is rather limited. The coefficients  $O(200 \text{ m}^2 \text{ s}^{-1})$  that are smaller than estimations from observations ( $O(10^3 \text{ m}^2 \text{ s}^{-1})$ ), such that there is finally some incoherence with the choice of the dyadic tensor  $\mathbf{A}$  in the ocean model should then be used. Following Cessi (2000), it is not clear how to attribute the variability to coupled processes or to simple oceanic turbulence. The clear criteria (like the phase relationship in poleward heat transport changes) are not clear. This is the challenge of climatic data analysis, so this might just be a first step.

## Conclusion

- Simplest setting for studying interactions between ocean gyres and zonal winds
- Potentially interesting mechanism for decadal oscillations observed in the North Pacific
- Further developments include the use of an ocean model that allow act as a boundary condition for temperature anomalies

## References

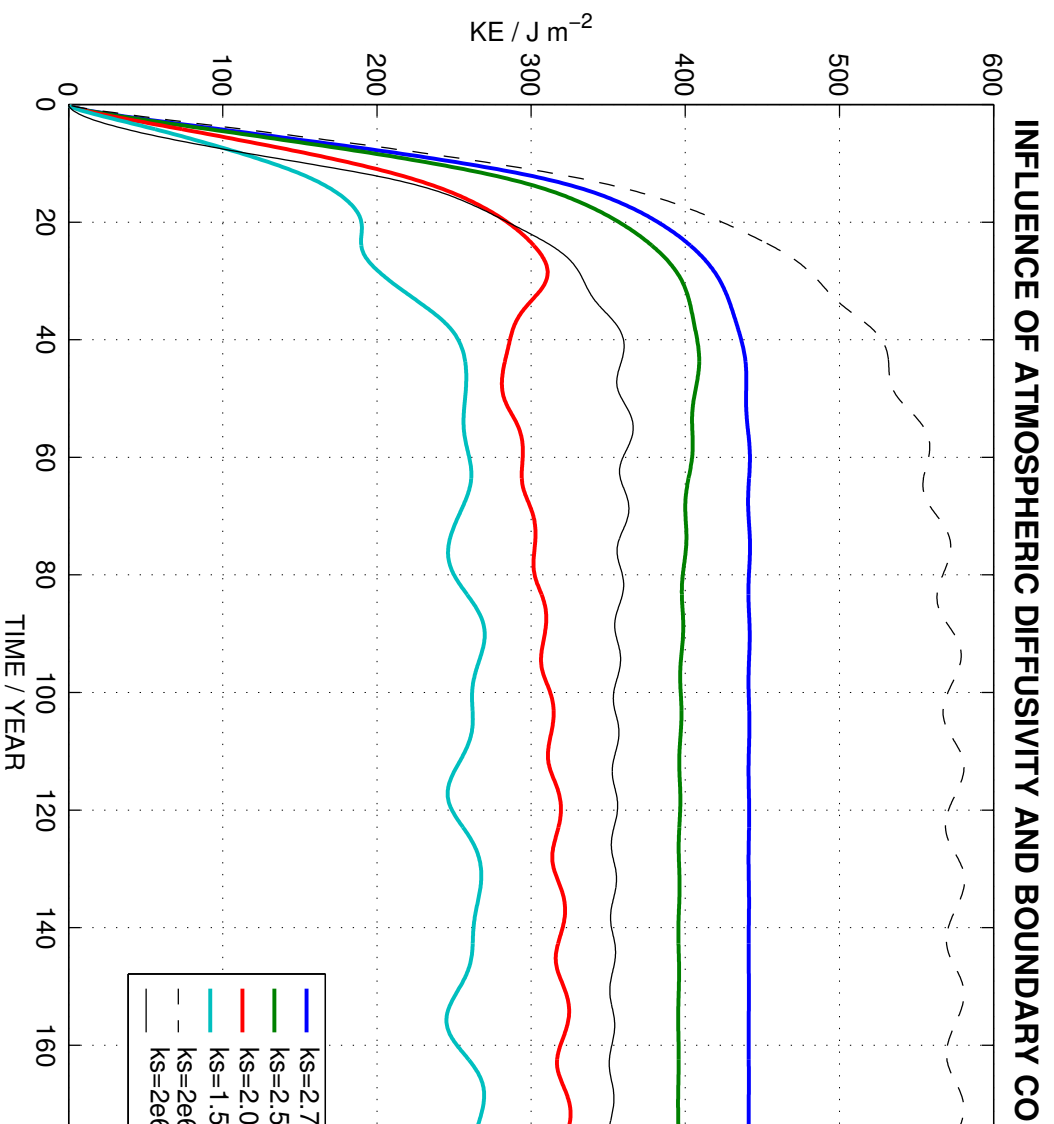
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pas [s]	time [yr]	period [yr]	$KE_{min}$ [J m <sup>-2</sup> ]	$KE_{max}$ [J m <sup>-2</sup> ]	$SST_{min}$ [°C]	$SST_{max}$ [°C]
3640	640	17.9	454	465	-51.28	121.18
3640	500	18.4	539	550	-40.29	91.49
7200	280	18.9	553	565	-34.41	77.16
3800	210	19.2	563	574	-30.74	68.49
2000	202	19.5	569	581	-28.01	62.82
3640	620	EQ.	517	517	-40.86	114.53
3640	668	EQ.	557	557	-31.72	89.43
7200	270	EQ.	573	573	-27.15	75.48
3800	916	EQ.	583	583	-24.18	67.02
1920	200	EQ.	590	591	-22.13	61.54
1080	200	EQ.	605	605	-18.04	51.33

periments summary:  $A_x = 2000 \text{ m}^2 \text{ s}^{-1}$ ,  $A_y = K = 200 \text{ m}^2 \text{ s}^{-1}$ ,  $\tau = 0$  s in Cessi (2000). Note the influence of resolution on the extrema in

Option	Typical value
viscosity parameter	$10^{-4} \text{ s}^{-1}$
baroclinic eddy $\beta$ -effect	$1.6 \times 10^{-11} \text{ m}^{-1} \text{ s}^{-1}$
heat for air	$1000 \text{ J K}^{-1} \text{ kg}^{-1}$
heat for sea water	$4000 \text{ J K}^{-1} \text{ kg}^{-1}$
zonal extent	$0.825 \times 10^7 \text{ m}$
meridional extent	$1.0 \times 10^7 \text{ m}$
thermocline height	$8 \times 10^3 \text{ m}$
thermocline depth	$10^3 \text{ m}$
air density	$1.25 \text{ kg m}^{-3}$
water density	$1000 \text{ kg m}^{-3}$
atmosphere exchange coefficient	$23 \text{ W m}^{-2} \text{ K}^{-1}$
drag coefficient	$2.4 \times 10^{-2} \text{ m s}^{-1}$
surface gravity	$9.8 \text{ m s}^{-2}$
mean temperature	$273 \text{ K}$
thermic stratification	$5 \times 10^{-3} \text{ K m}^{-1}$
fraction of atmosphere above ocean	$0.3$
infrared radiation (LW) for $\theta = 0^\circ \text{C}$	$200 \text{ W m}^{-2}$
$\partial \text{LW} / \partial \theta$	$2.475 \text{ W m}^{-2} \text{ }^\circ\text{C}^{-1}$
thermic surface baroclinic eddy diffusivity	$2 - 3 \times 10^6 \text{ m}^2 \text{ s}^{-1}$
baroclinic eddy diffusivity	$200 - 2000 \text{ m}^2 \text{ s}^{-1}$
eddy-viscosity	$200 - 2000 \text{ m}^2 \text{ s}^{-1}$

Table 2: Parameters used in the coupled model



Time series of kinetic energy for various experiments with different values of boundary conditions (KS) and for different boundary conditions for wind speed (KS)